

Collaborators

V. Křápek

IoP Prague

V. I. Anisimov, A. V. Lukoyanov,
D. M. Korotin, M. A. Korotin

IoMP Yekaterinburg

P. Werner

ETH Zurich

W. E. Pickett, R. T. Scalettar

UC Davis

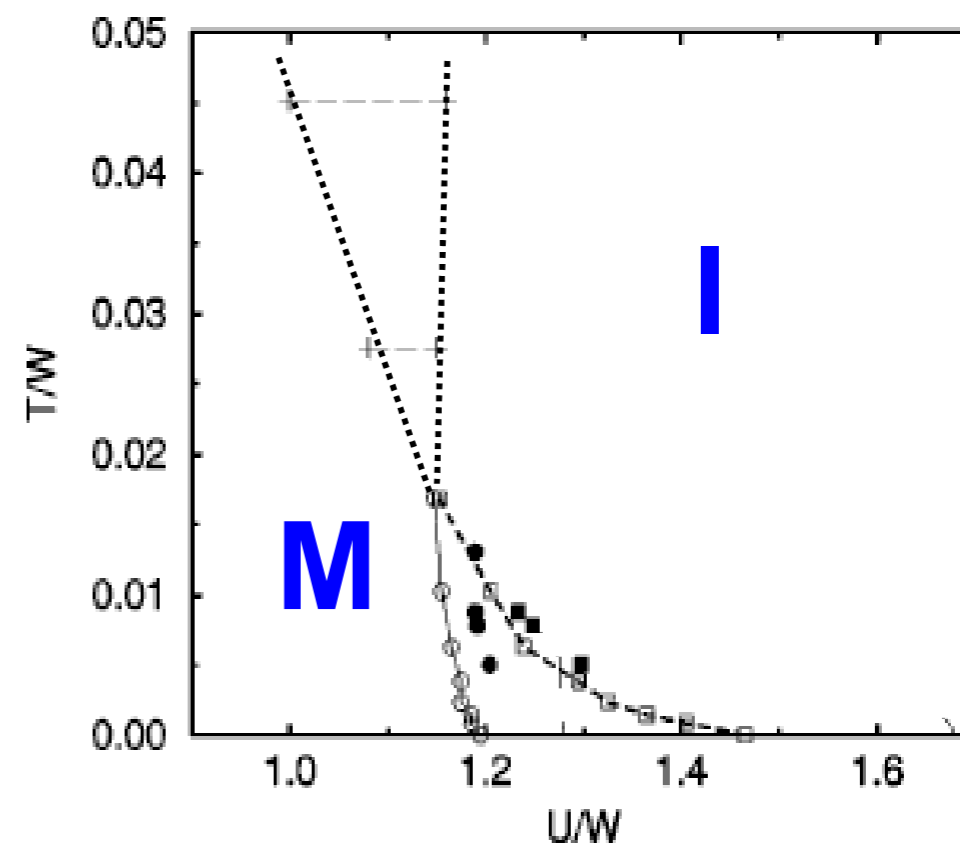
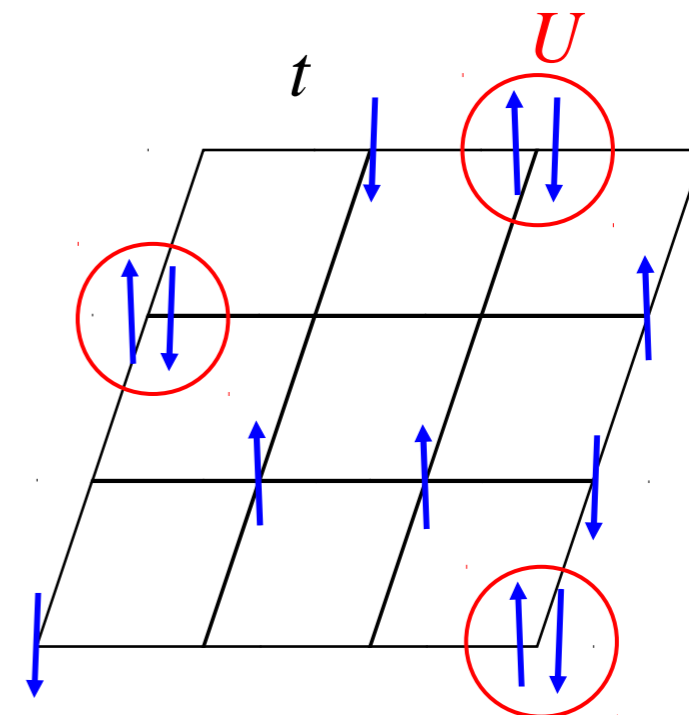
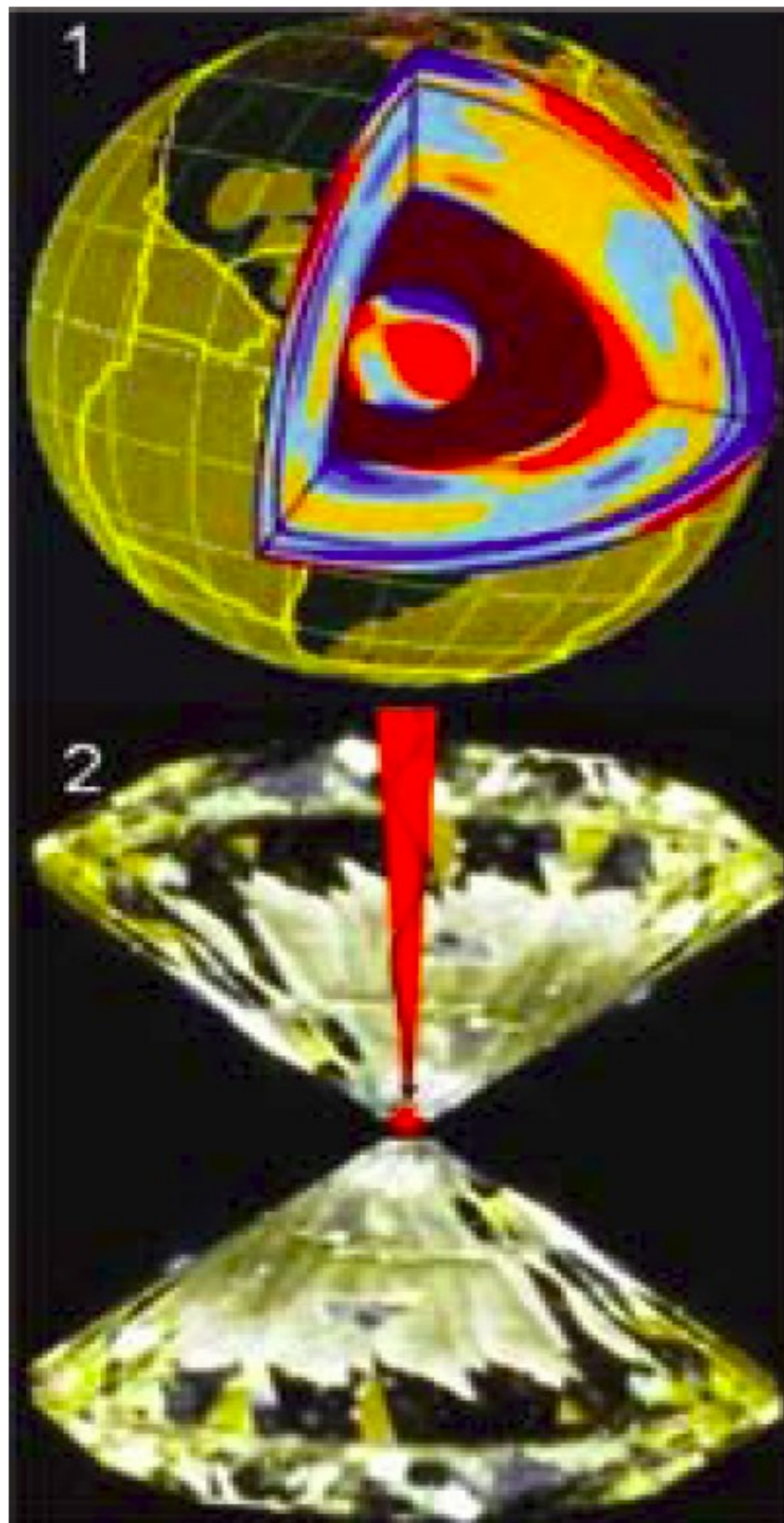
Outline

- HS-LS transitions in models and materials
- Pressure-driven transition: MnO , Fe_2O_3
- HS/LS degeneracy: LaCoO_3
- Blume-Emery-Griffiths model in fermionic systems
- From cobaltites to manganites
- Conclusions

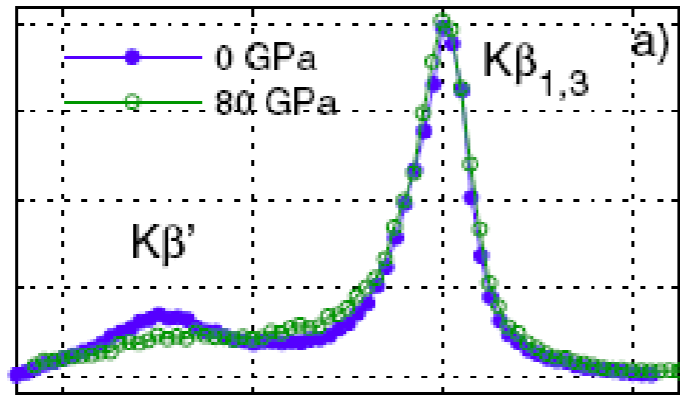
Materials



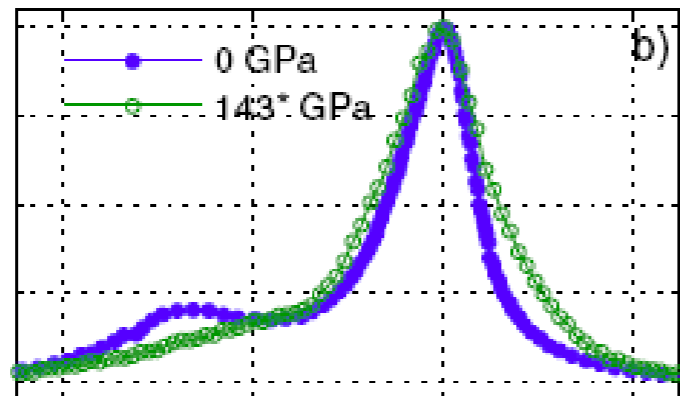
Models



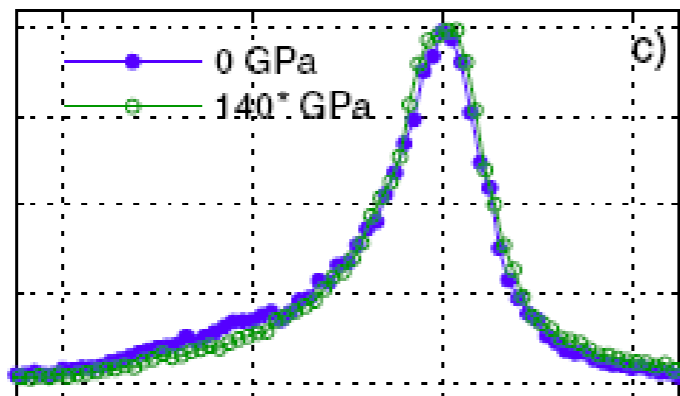
MnO



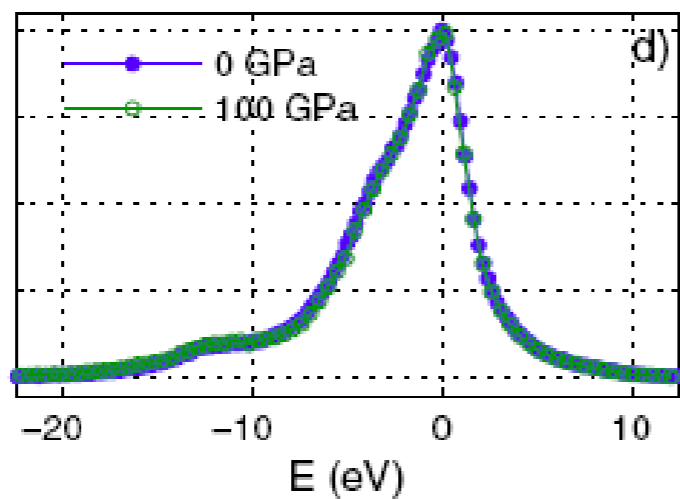
FeO



CoO



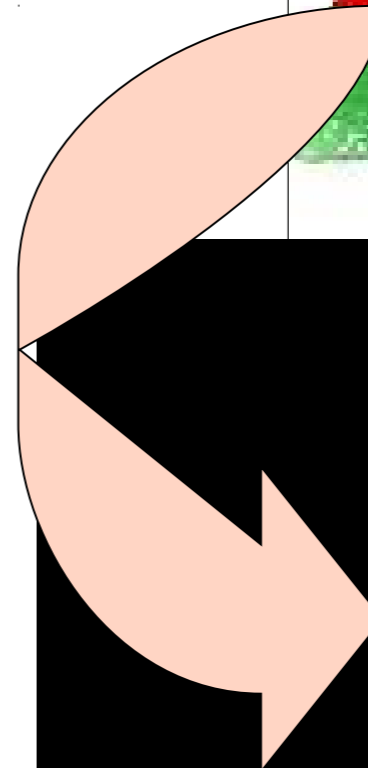
NiO



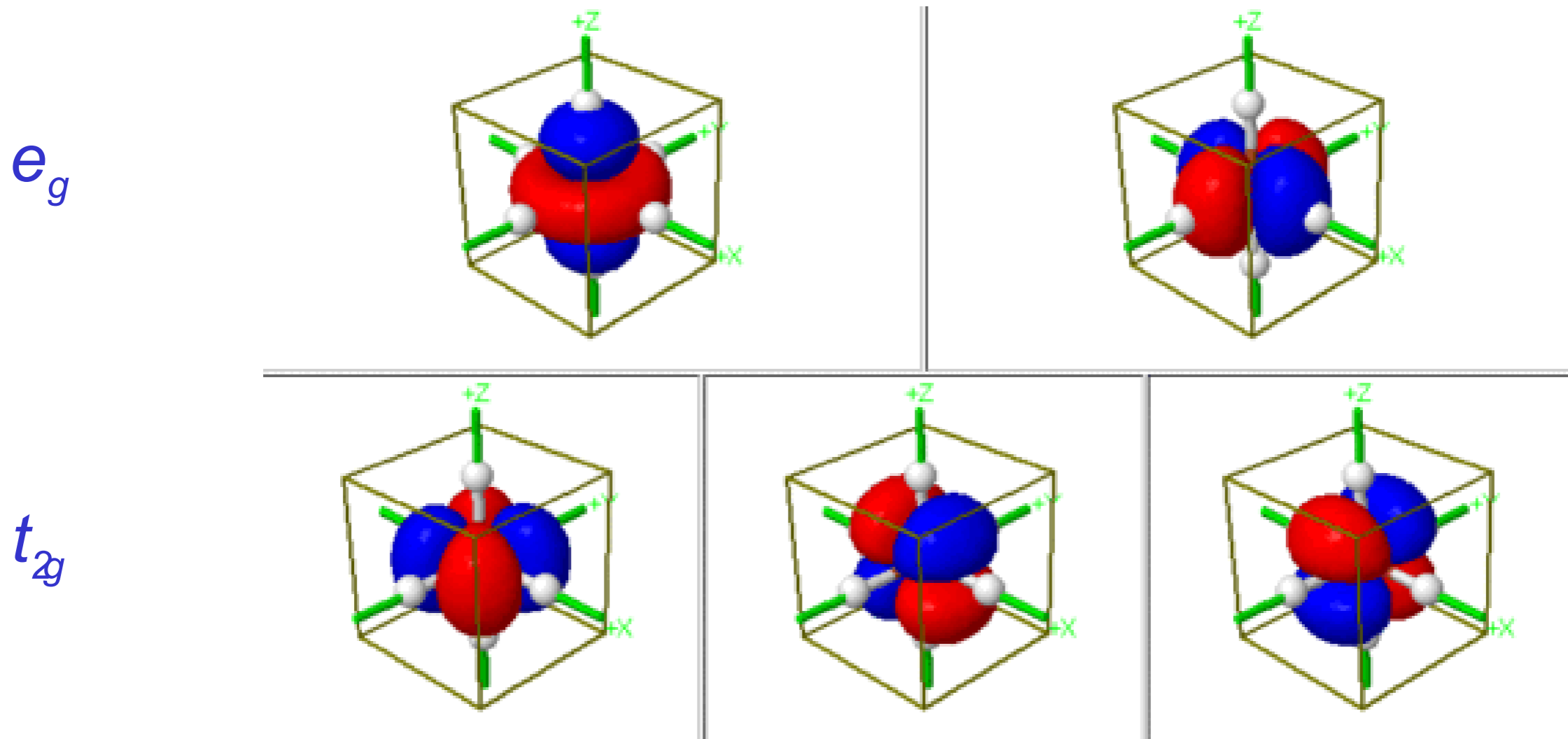
MnO



Pressure



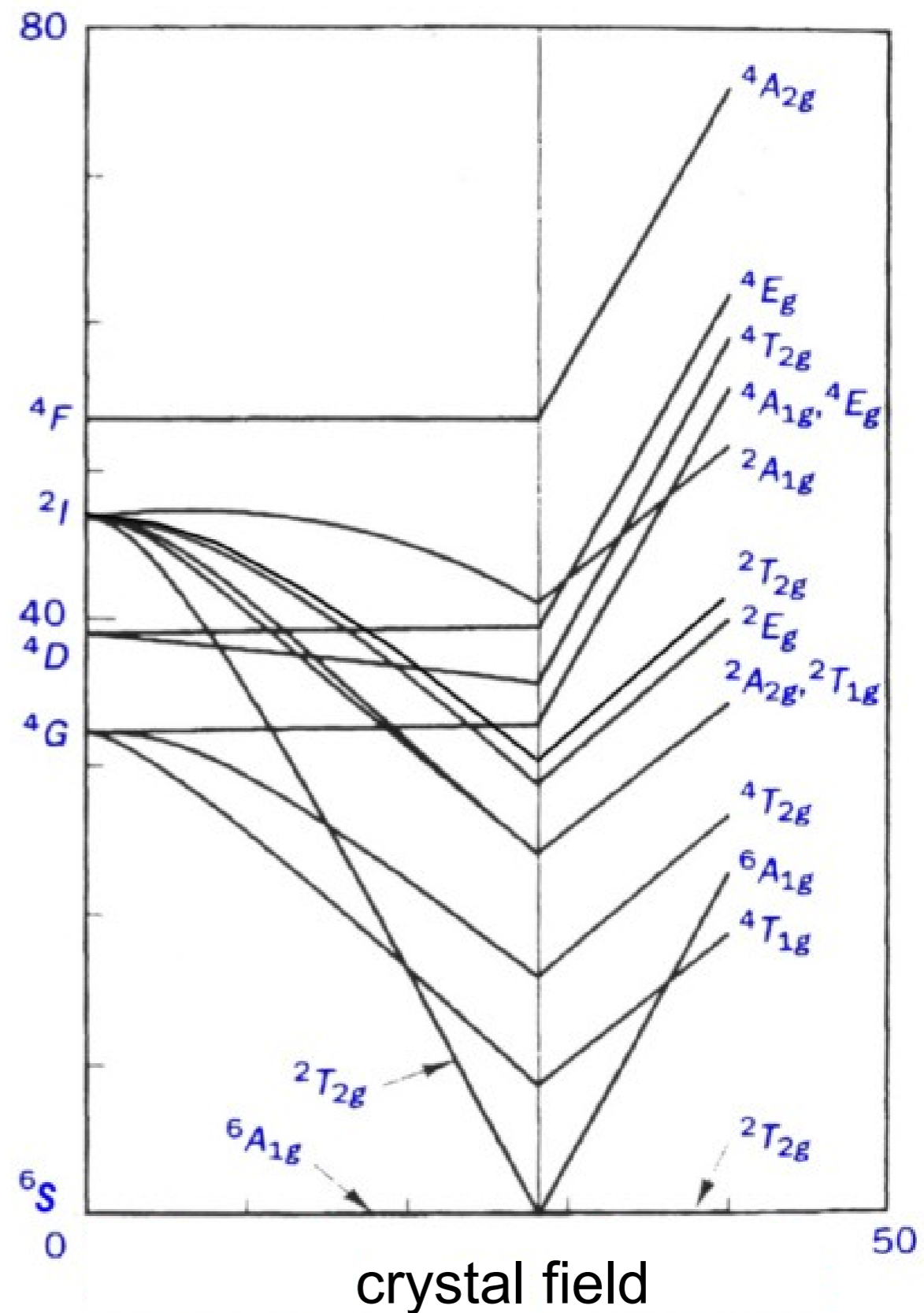
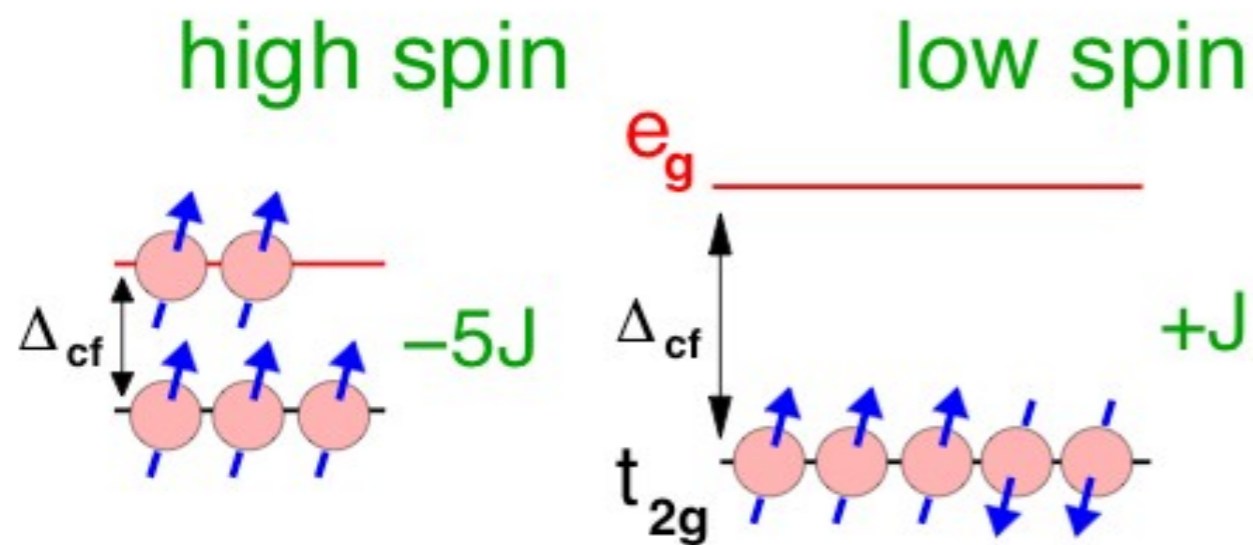
d-electron in octahedral environment



Crystal-field splitting: electrostatic forces
hybridization (band repulsion)

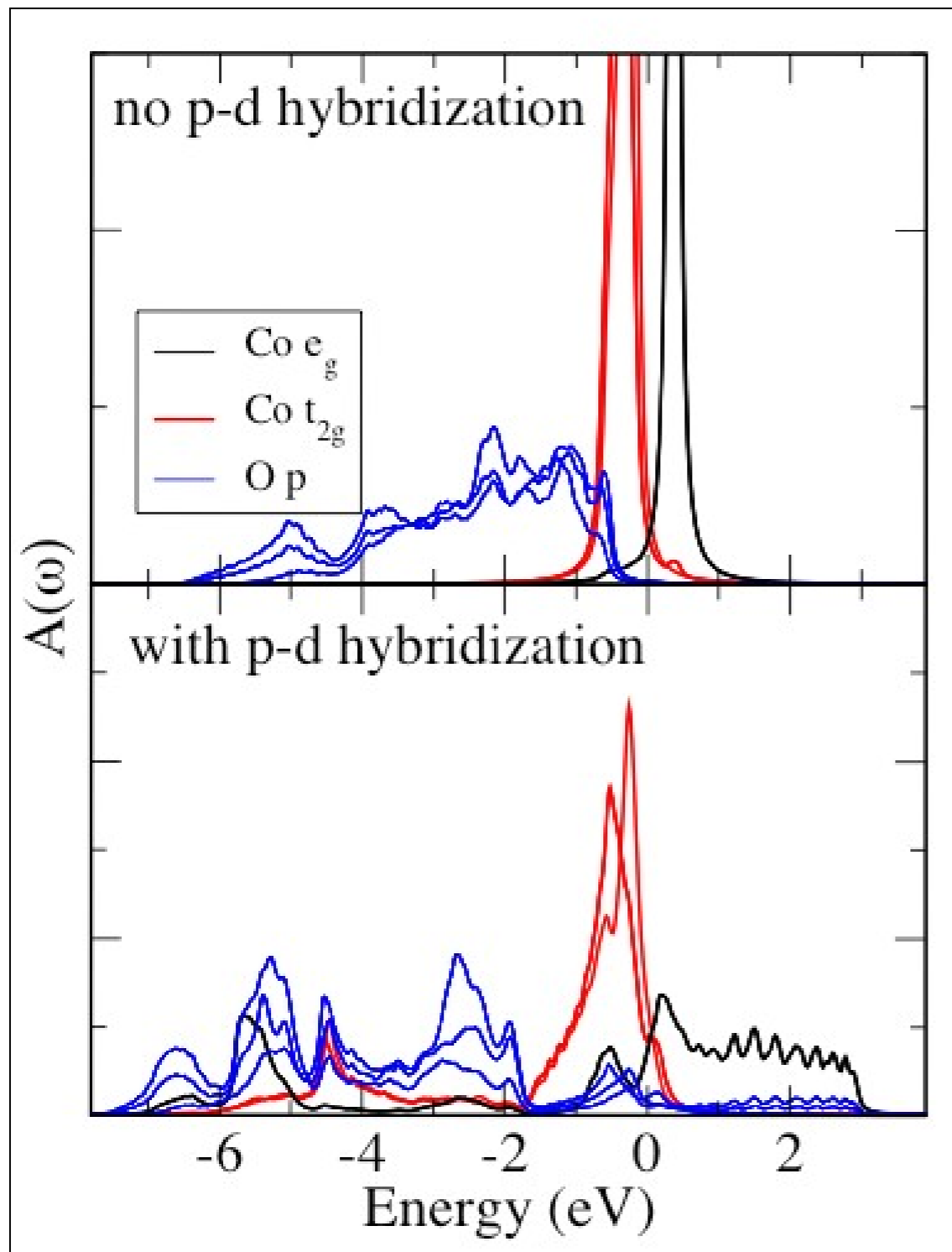
d-multiplets in octahedral field

Tanabe-Sugano diagram for d^5



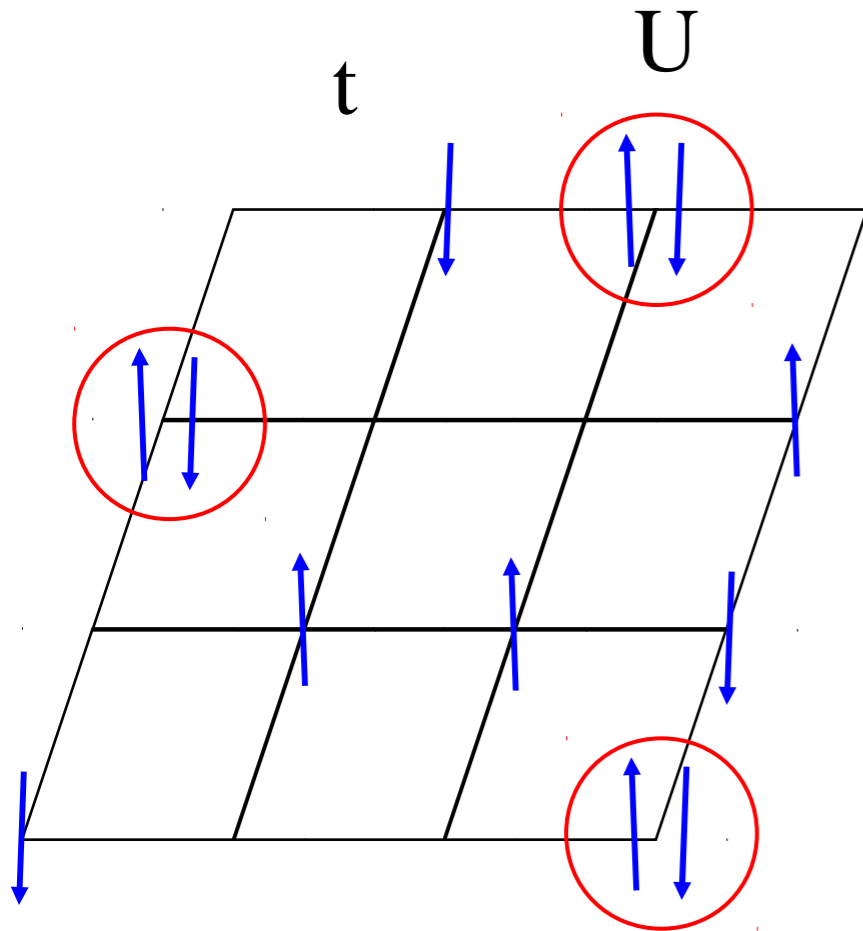
Transition metal oxides- band structure

LDA bands for LaCoO_3



- hopping from TM ions mostly through oxygen
- $p-e_g$ hybridization \Rightarrow broad e_g band
CF splitting
- relative position of d and p bands not necessarily correct

Electron correlations and Hubbard model

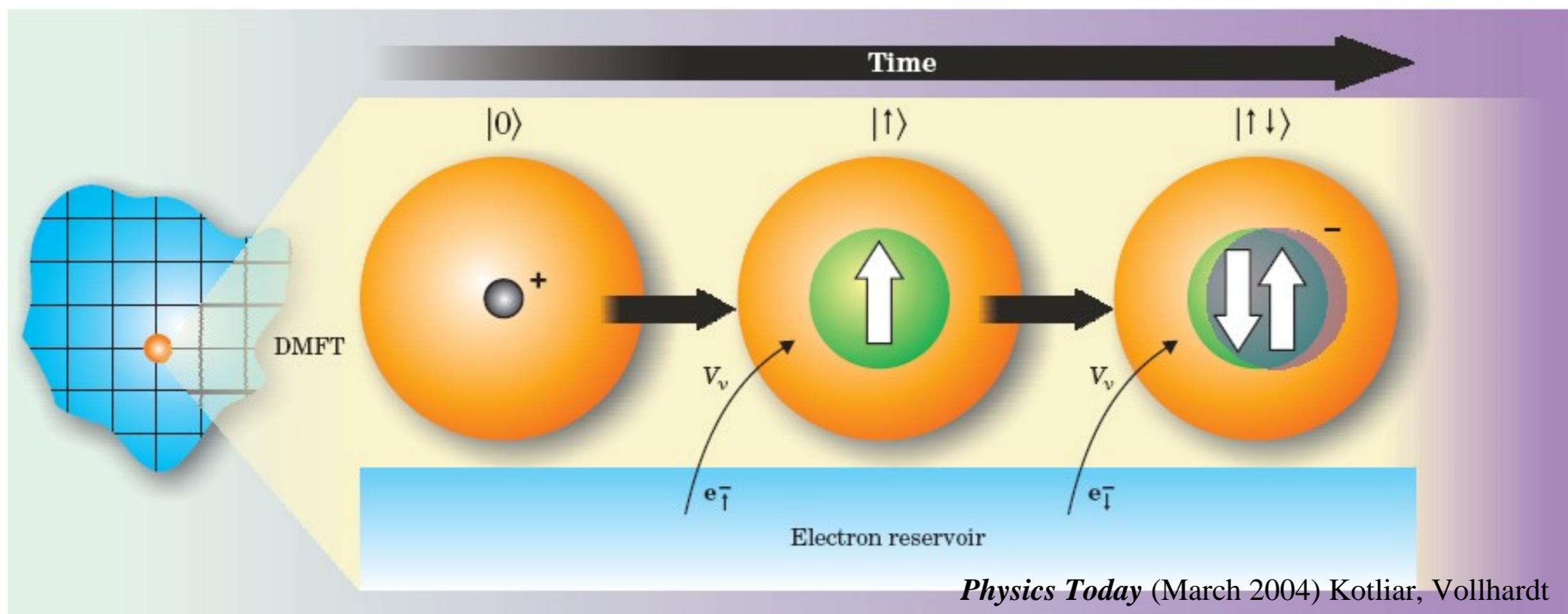
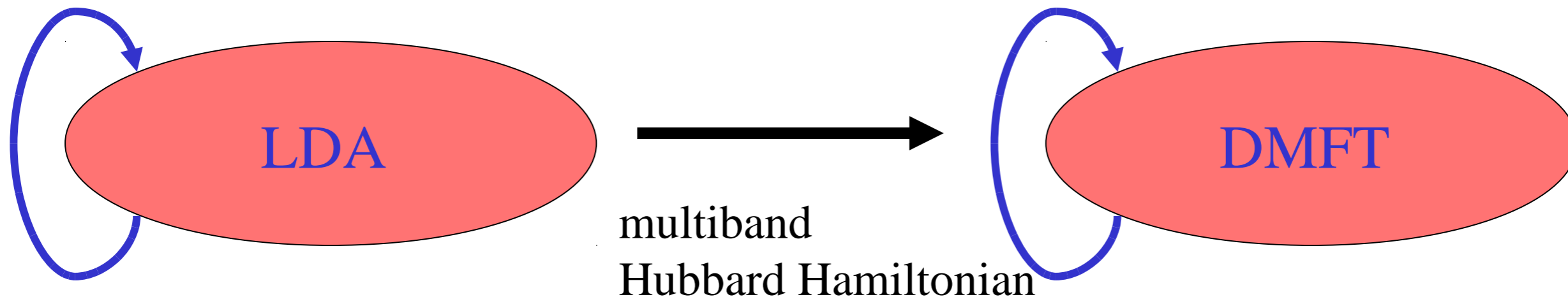


- competition between kinetic and interaction energy: itinerancy vs localization
- localization \rightarrow large (quasi)degeneracy \rightarrow temperature (entropy) becomes important parameter
- emergence - new (non-fermionic) degrees of freedom appear, e.g. local spin, orbital-pseudospin \rightarrow possibility of new ordered states
- fluctuations of the emergent degrees of freedom - both quantum mechanical and statistical

Dynamical Mean-Field Theory (LDA+DMFT)

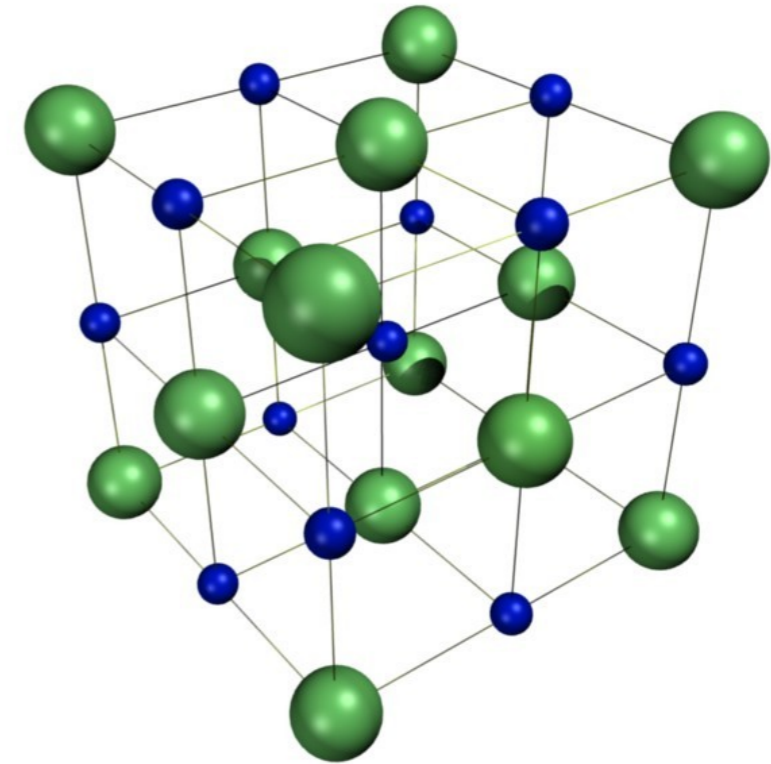
charge selfconsistency

many-body selfconsistency

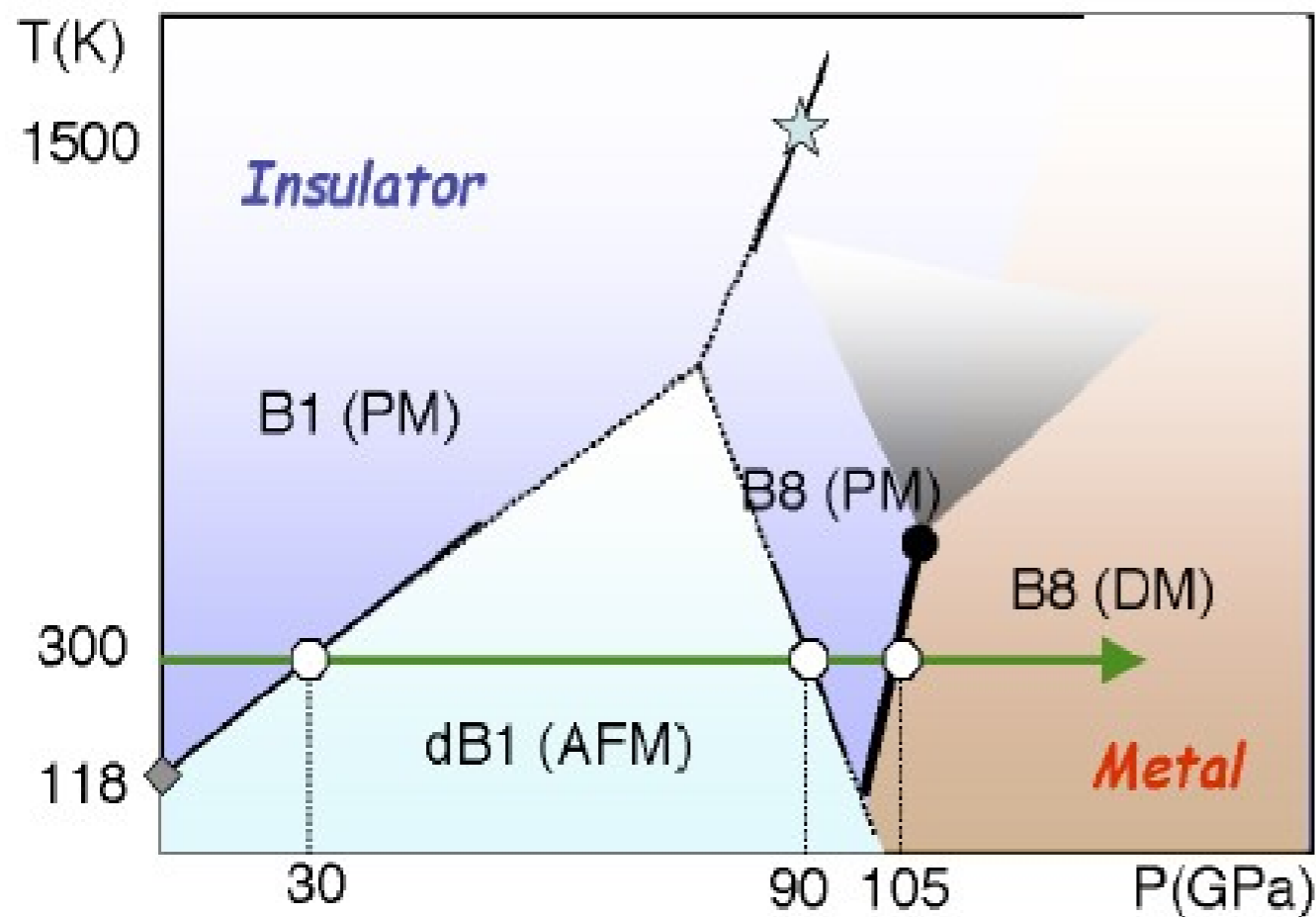


MnO experimental summary

$\text{Mn}^{2+} \text{O}^{2-} \Rightarrow d^5$ local configuration



Conceptual phase diagram of MnO

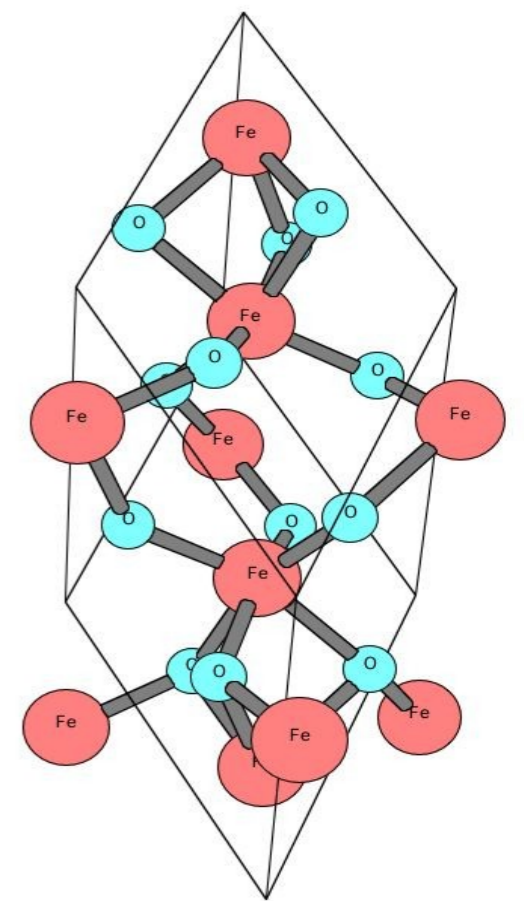


- moment collapse
- insulator \rightarrow metal transition
- volume collapse
- structural transition

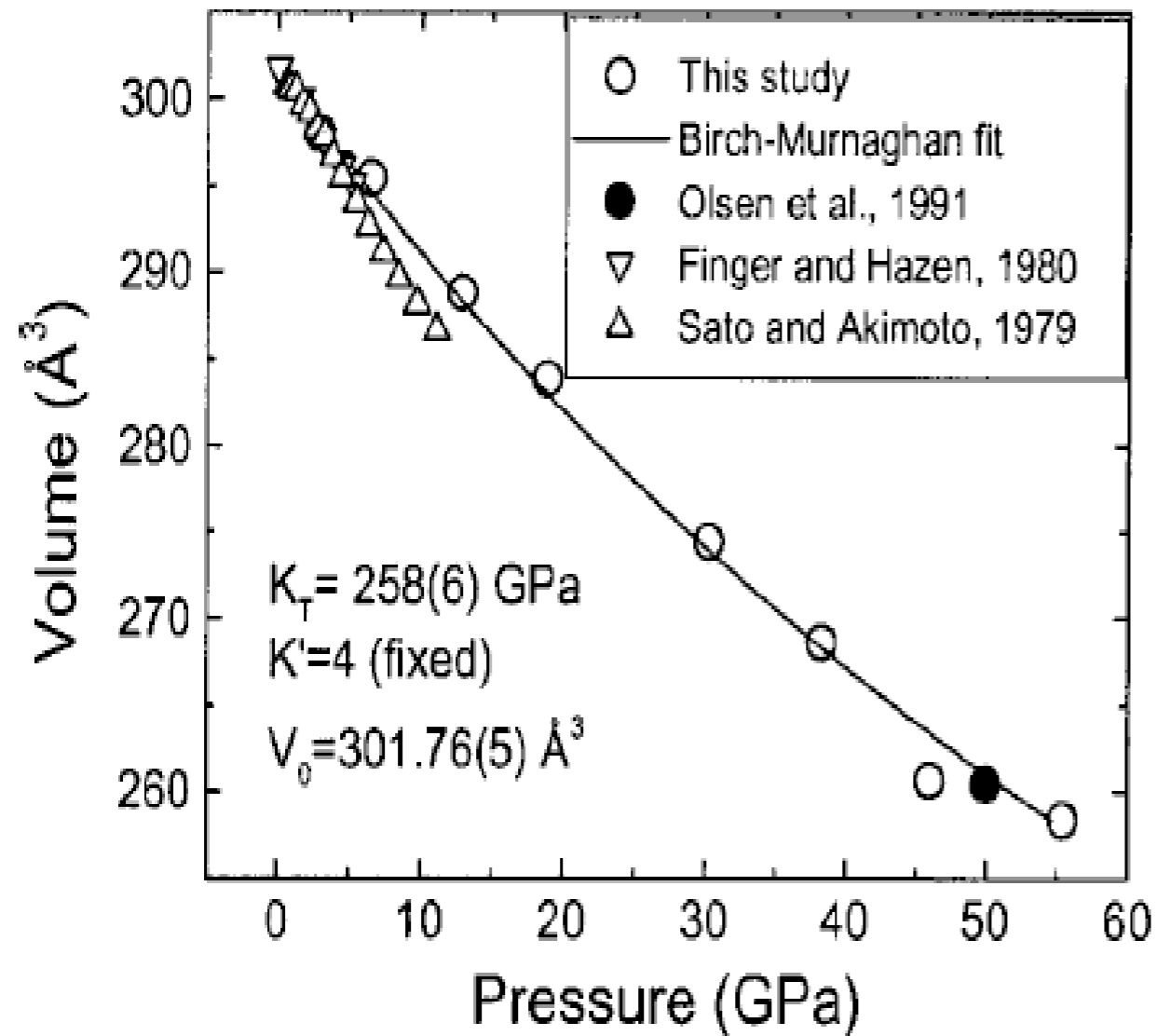
Fe₂O₃ experimental summary

Fe₂³⁺O₃²⁻ => d⁵ local configuration

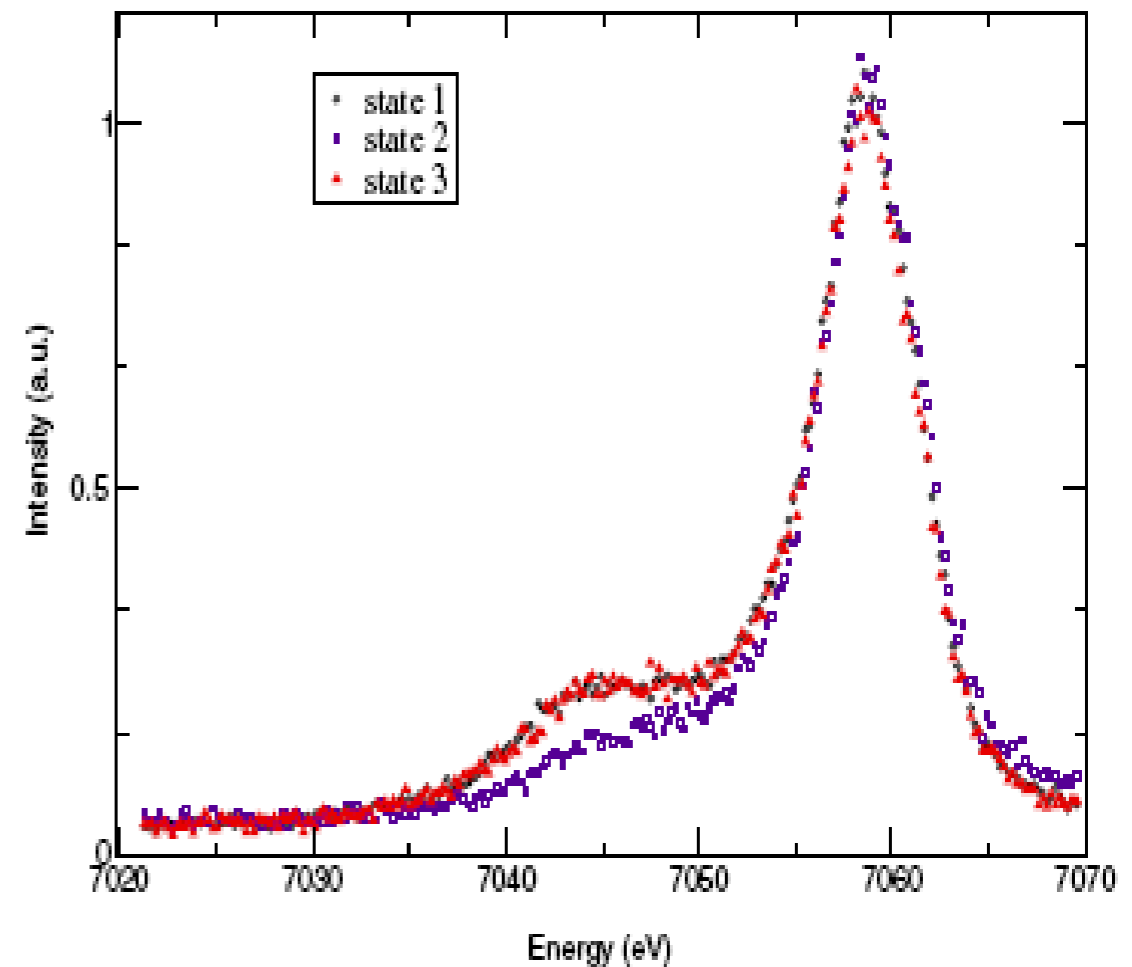
Fe in octahedral coordination



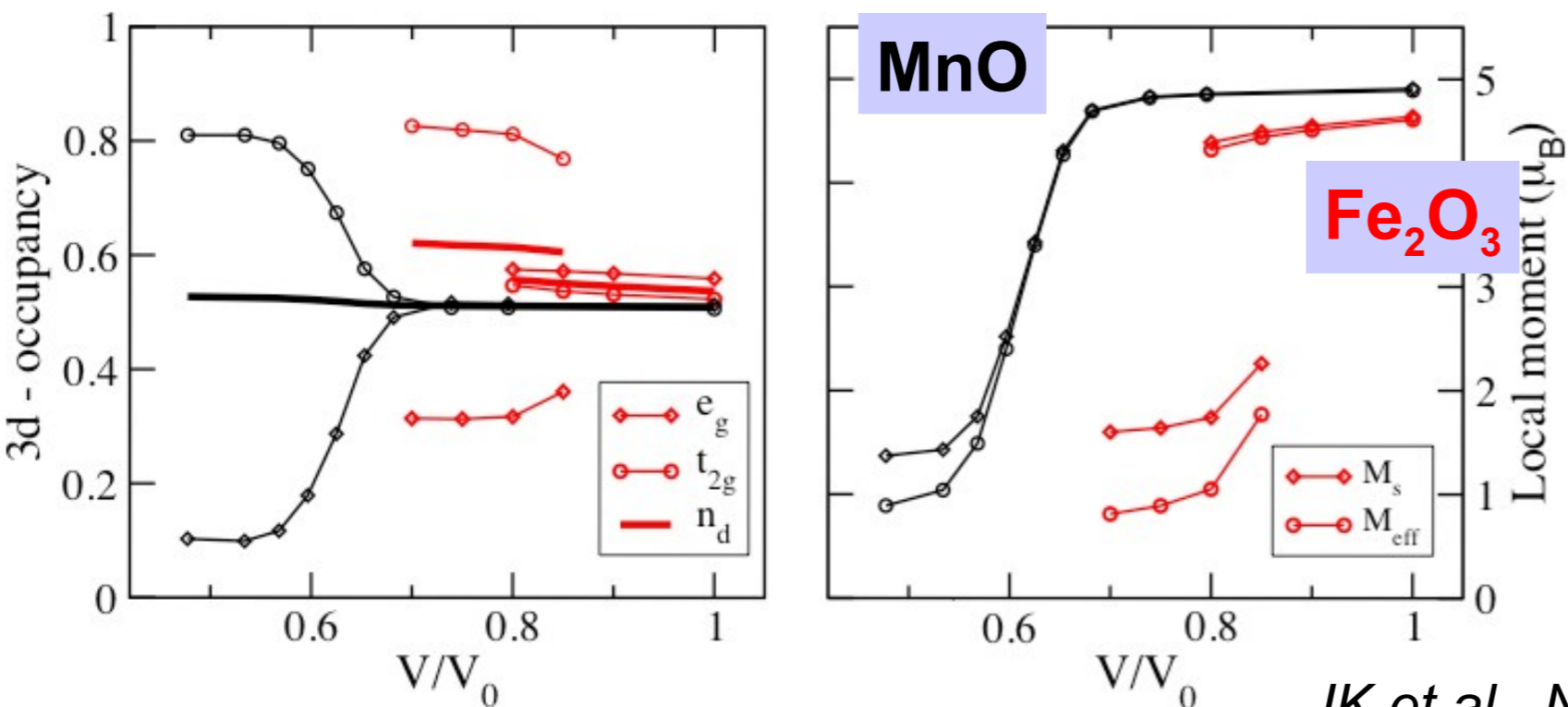
Rosenberg et al., *Phys. Rev. B* **65**, 064112 (2002)



Badro et al., *Phys. Rev. Lett.* **89**, 205504 (2002)



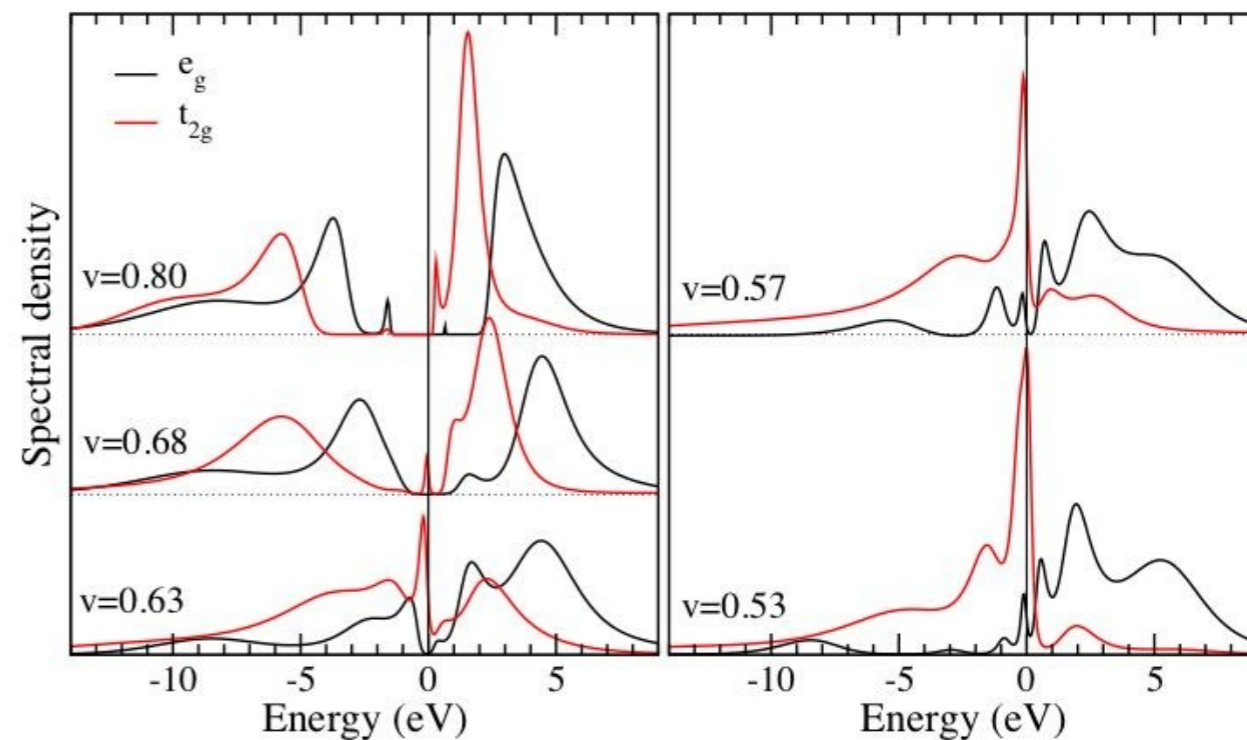
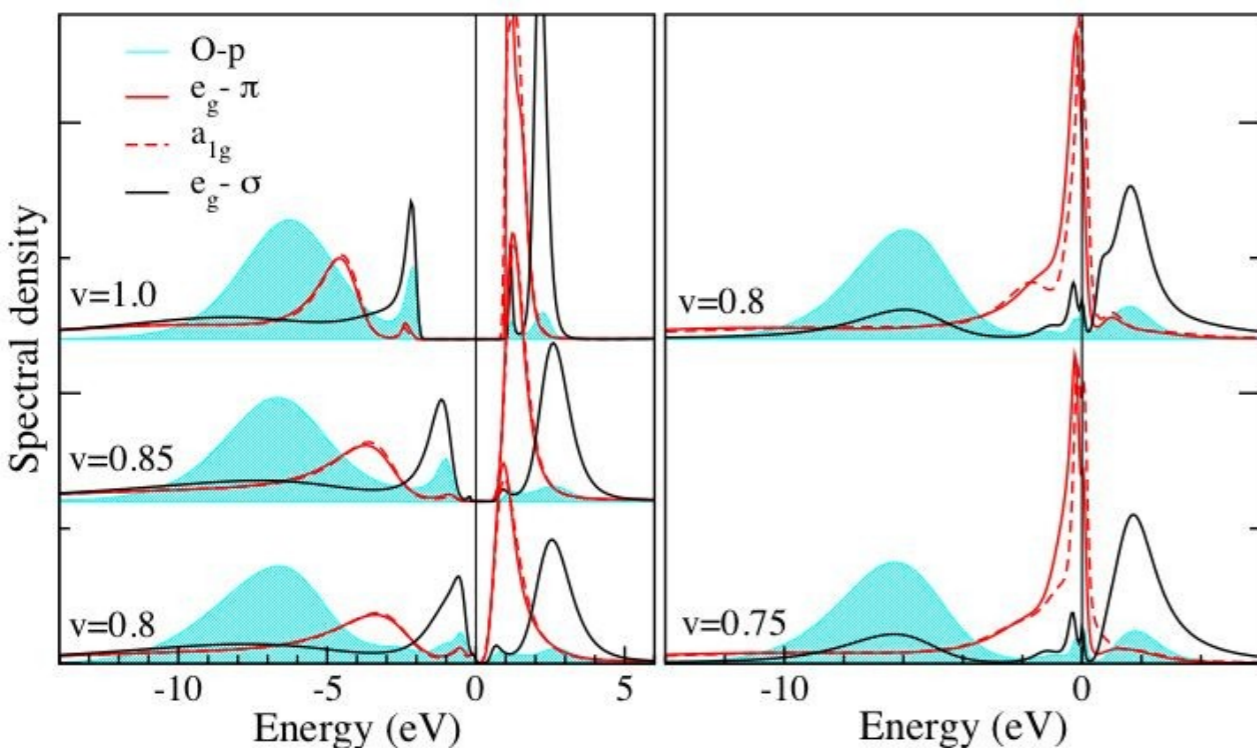
Pressure driven spin state transition



JK et al., Nature Materials 7, 198 (2008)
JK et al., Phys. Rev. Lett. 102, 146402 (2009)

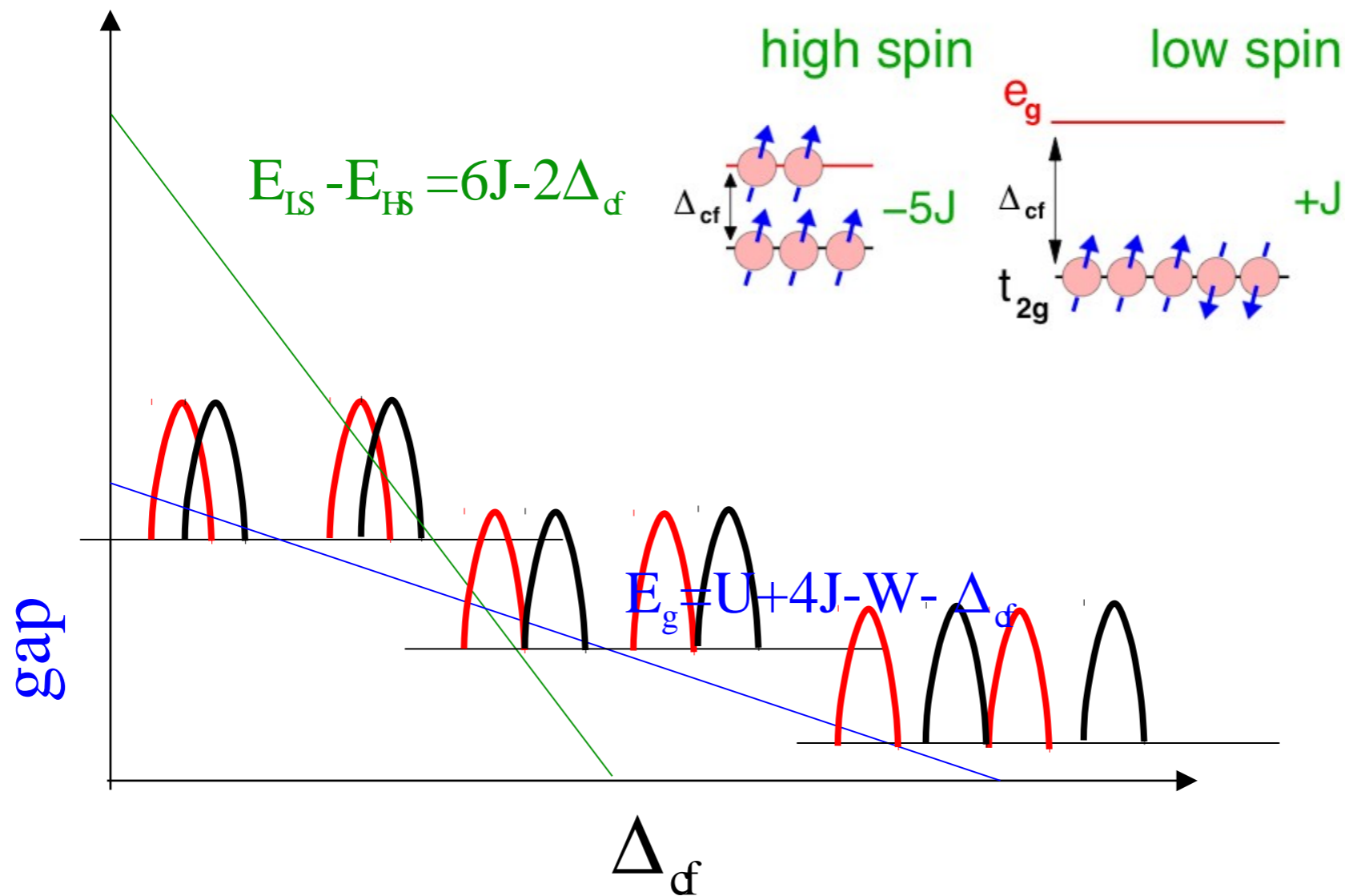
Fe₂O₃

MnO



Pressure induced metallization

Gap closing vs local spin state transition



Pressure induced transitions - summary

two scenarios:

- **local state transition** - atomic physics dominates
metallicity is slave to atomic constraints
- **gap closing** - hopping plays active role in the transition

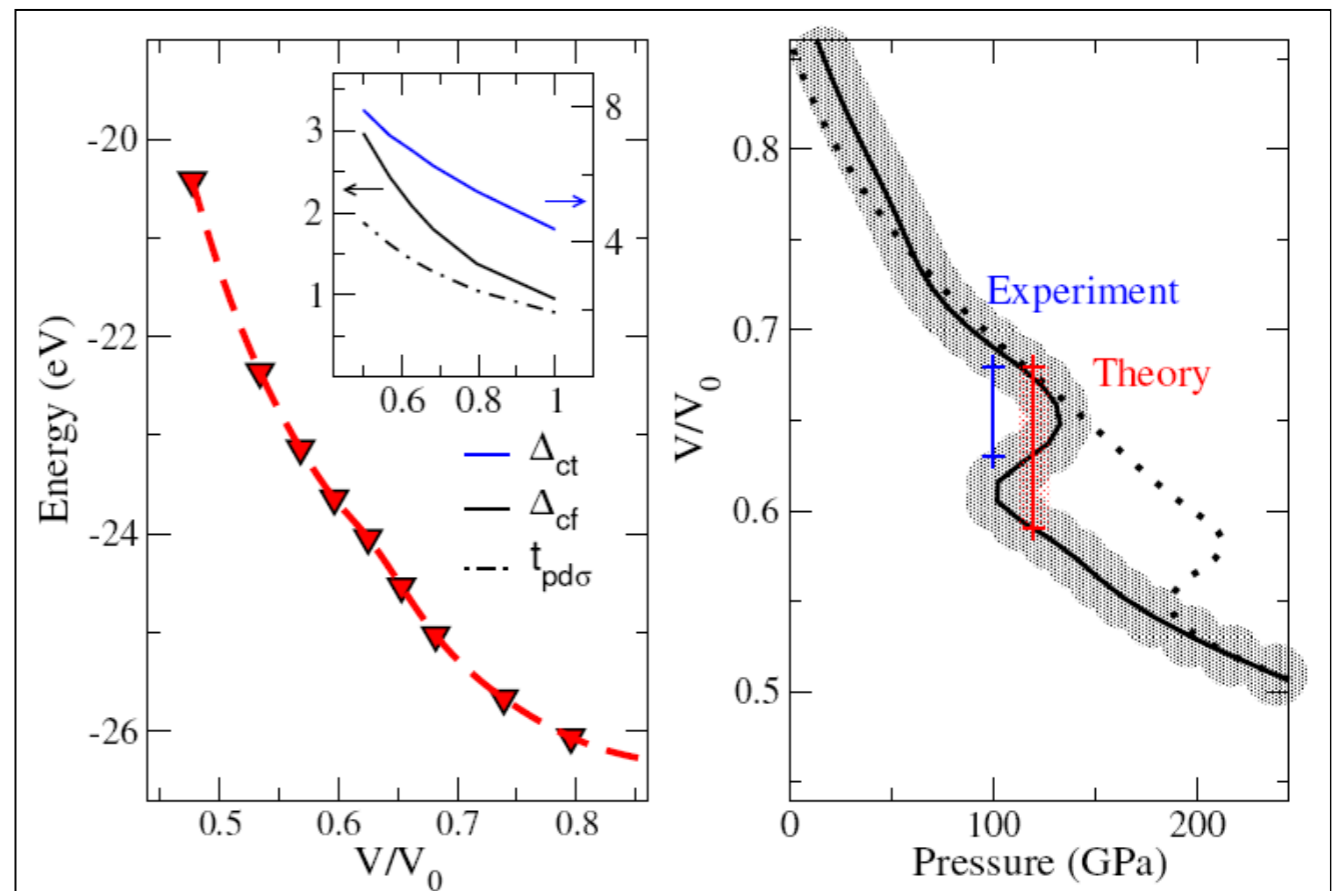
Energy scale:

~ 1 eV/atom

Pressure scale:

10-100 GPa

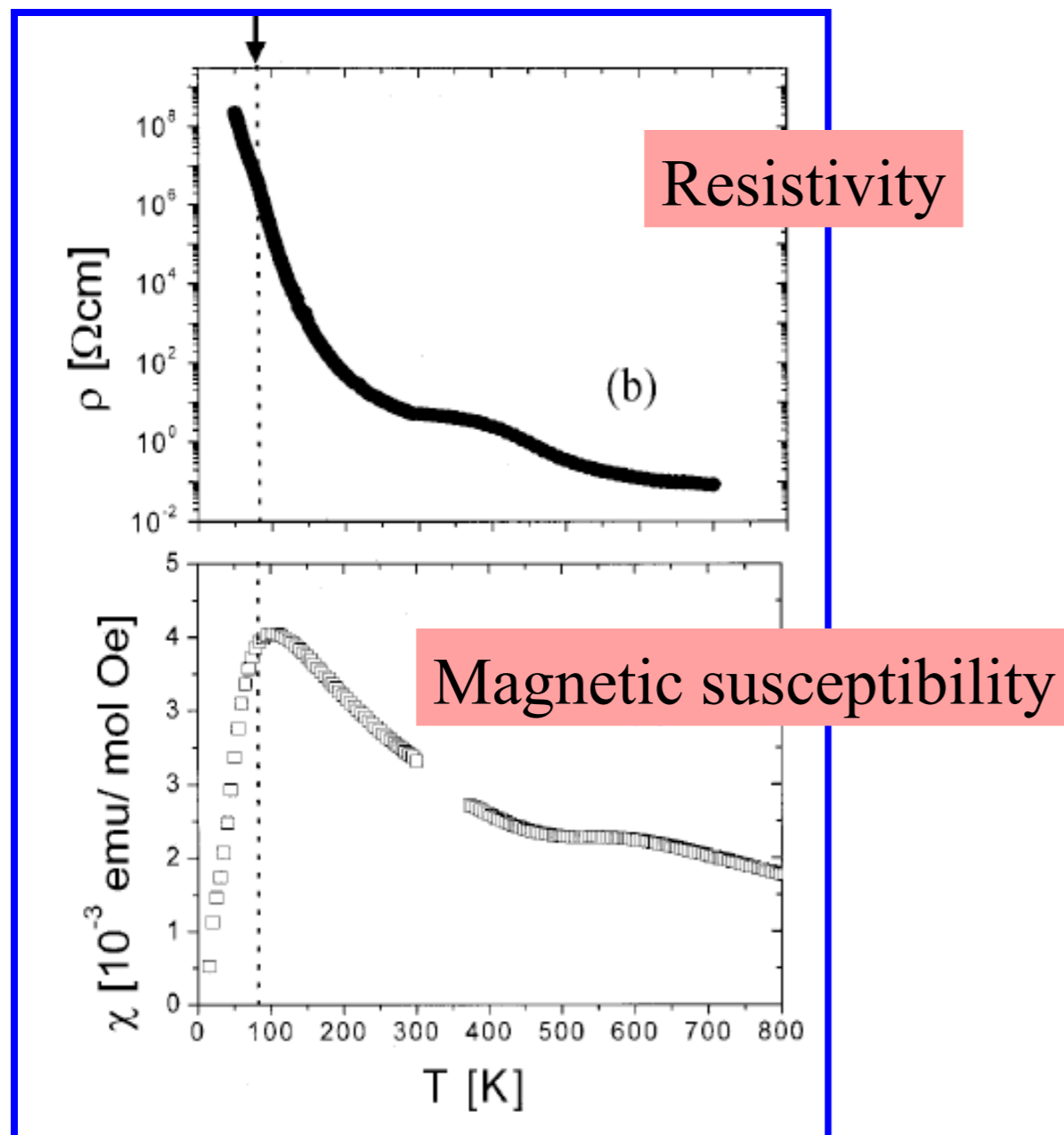
(~ 1 GPa width)



What happens right at the transition?

What happens right at the transition?

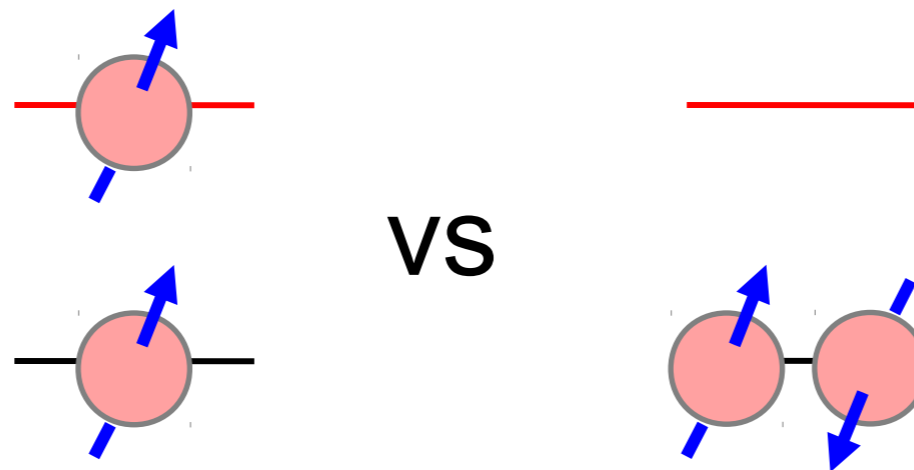
LaCoO₃ - nature did the fine tuning job for us !



- d^6 state for Co³⁺ valence
- $S=0$ LS vs $S=2$ or 1 ? HS
- $E_{\text{LS}} < E_{\text{HS}}$, $E_{\text{HS}} - E_{\text{LS}} \sim kT$

Two-band Hubbard model

$$\begin{aligned}
 H = & \sum_{i,\sigma} ((\Delta - \mu)n_{i,\sigma}^a - \mu n_{i,\sigma}^b) + \sum_{\langle ij \rangle, \sigma} (t_{aa} a_{i,\sigma}^\dagger a_{j,\sigma} + t_{bb} b_{i,\sigma}^\dagger b_{i,\sigma}) \\
 & + U \sum_i (n_{i,\uparrow}^a n_{i,\downarrow}^a + n_{i,\uparrow}^b n_{i,\downarrow}^b) + (U - 2J) \sum_{i,\sigma} n_{i,\sigma}^a n_{i,-\sigma}^b \\
 & + (U - 3J) \sum_{i,\sigma} n_{i,\sigma}^a n_{i,\sigma}^b
 \end{aligned}$$

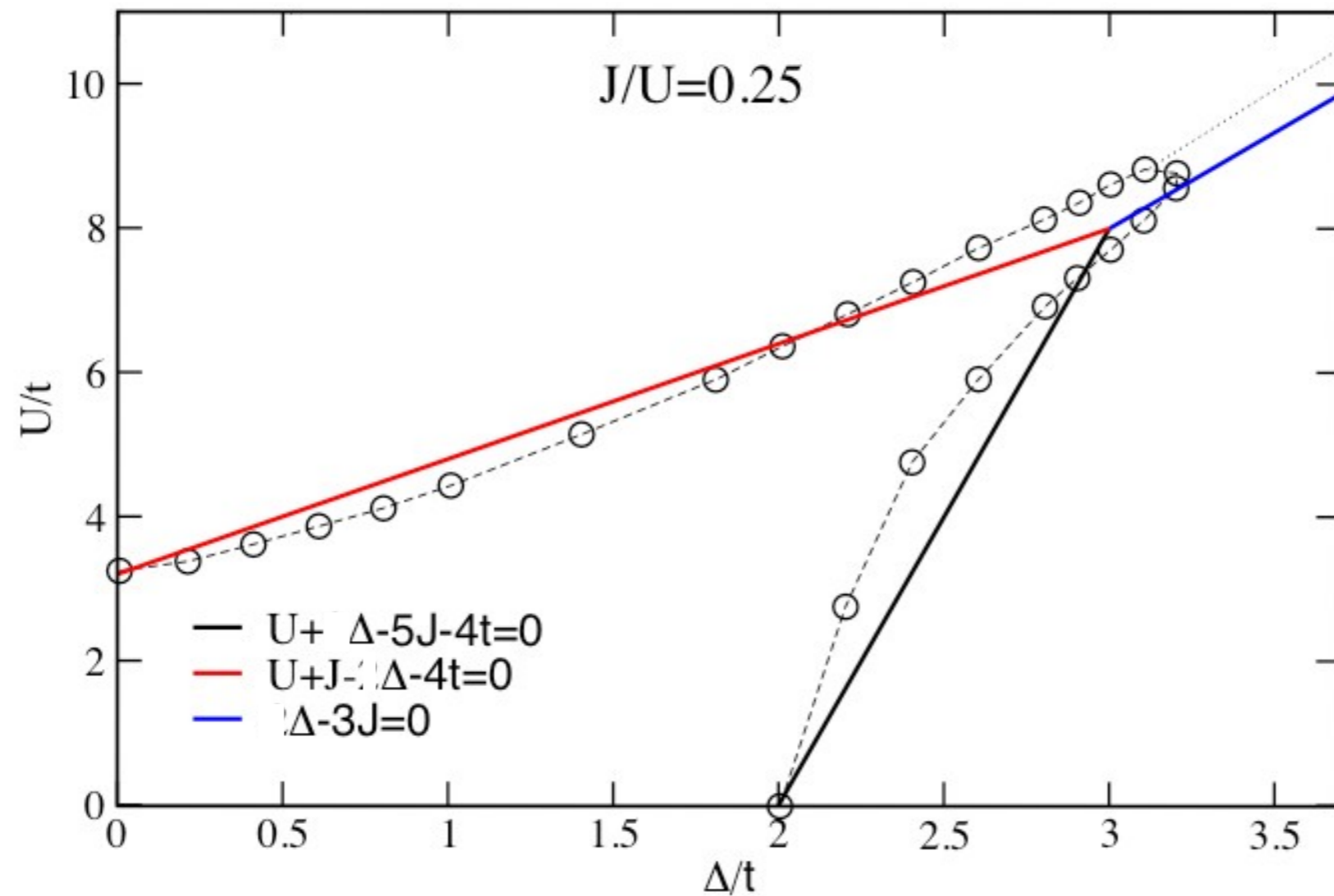


U- Δ phase diagram

Δ - crystal field

J/U - fixed

2D - bipartite lattice (square lattice)



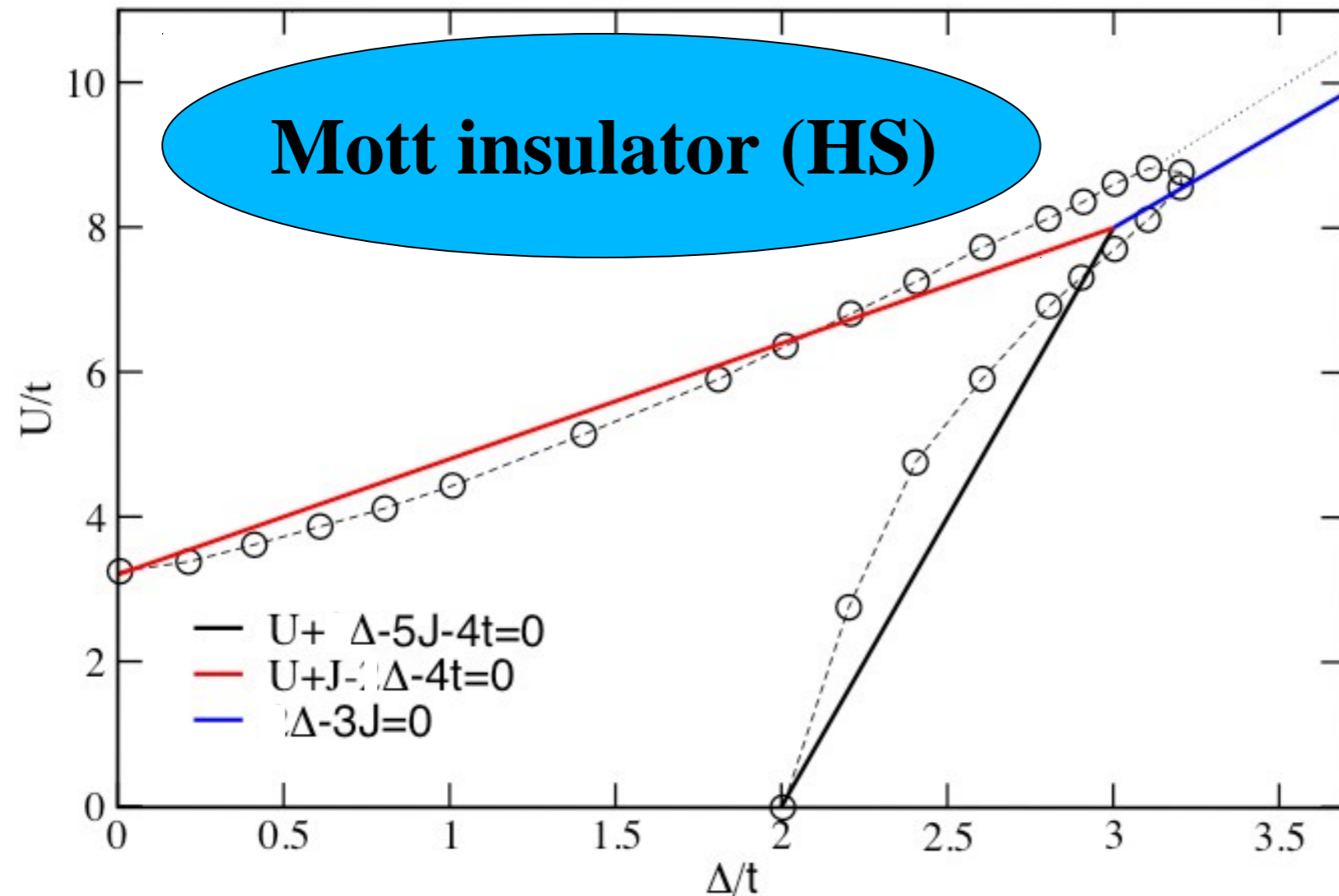
Werner & Millis, *Phys. Rev. Lett.* **99**, 126405 (2007)
JK et al. *Eur. Phys. J. Special Topics* **180**, 5 (2009)

U- Δ phase diagram

Δ - crystal field

J/U - fixed

2D - bipartite lattice (square lattice)



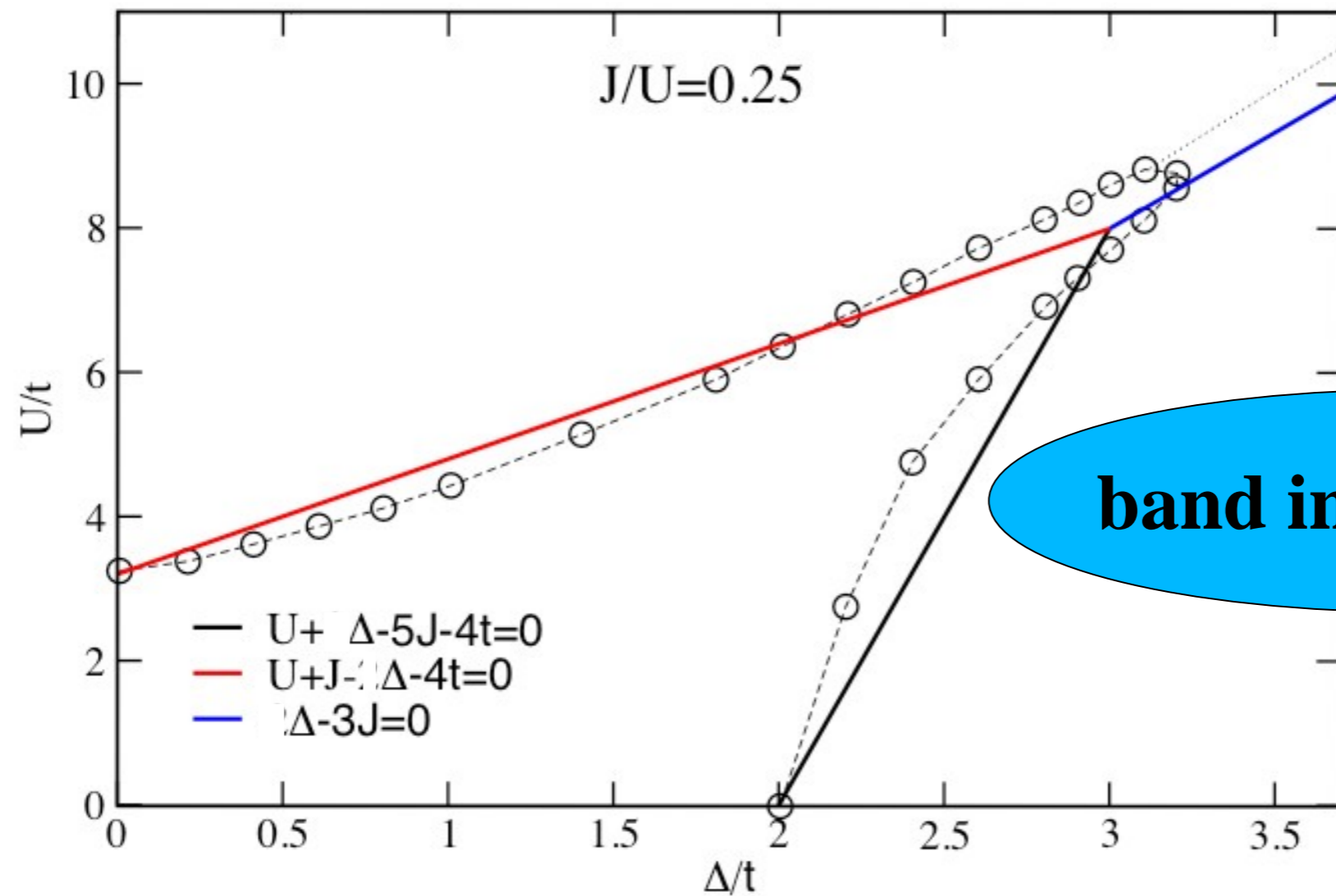
Werner & Millis, *Phys. Rev. Lett.* **99**, 126405 (2007)
JK et al. *Eur. Phys. J. Special Topics* **180**, 5 (2009)

U- Δ phase diagram

Δ - crystal field

J/U - fixed

2D - bipartite lattice (square lattice)



band insulator (LS)

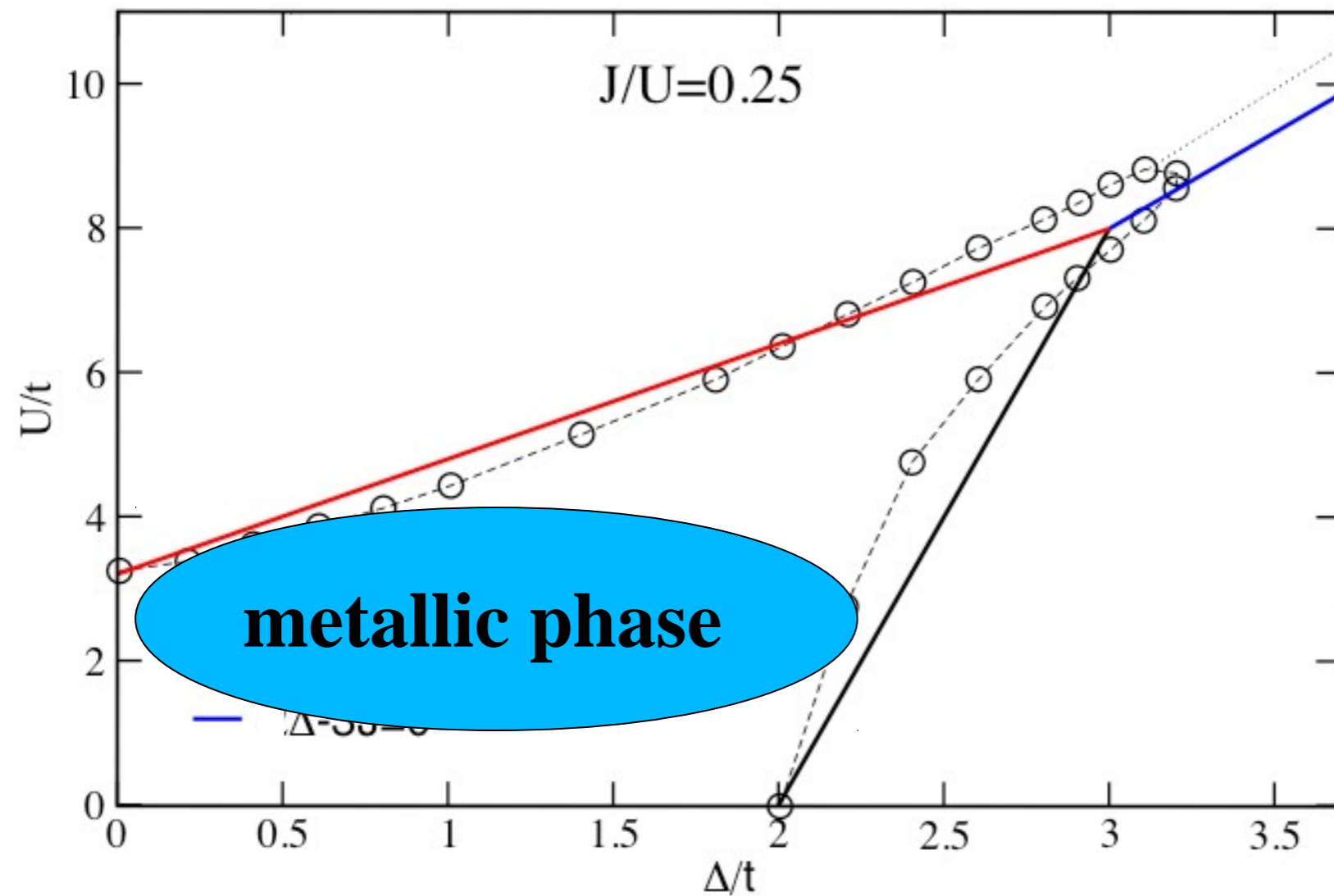
Werner & Millis, *Phys. Rev. Lett.* **99**, 126405 (2007)
JK et al. *Eur. Phys. J. Special Topics* **180**, 5 (2009)

U- Δ phase diagram

Δ - crystal field

J/U - fixed

2D - bipartite lattice (square lattice)

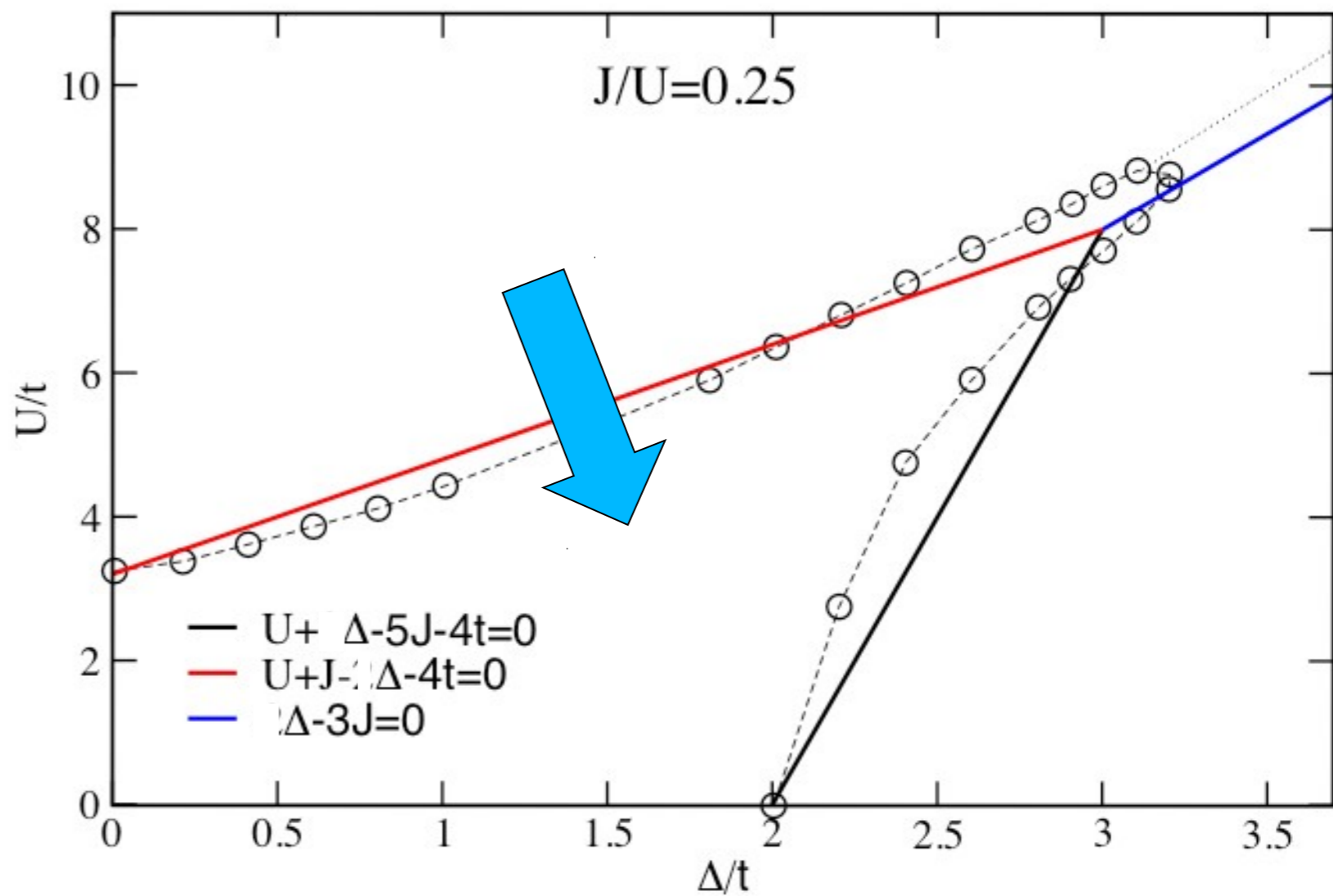
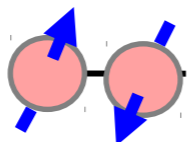
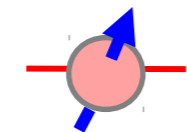
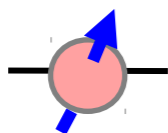
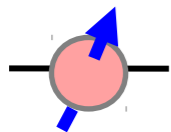
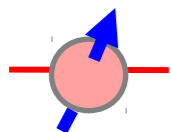


Werner & Millis, *Phys. Rev. Lett.* **99**, 126405 (2007)
JK et al. *Eur. Phys. J. Special Topics* **180**, 5 (2009)

Gap closing

'Mott gap = 0'

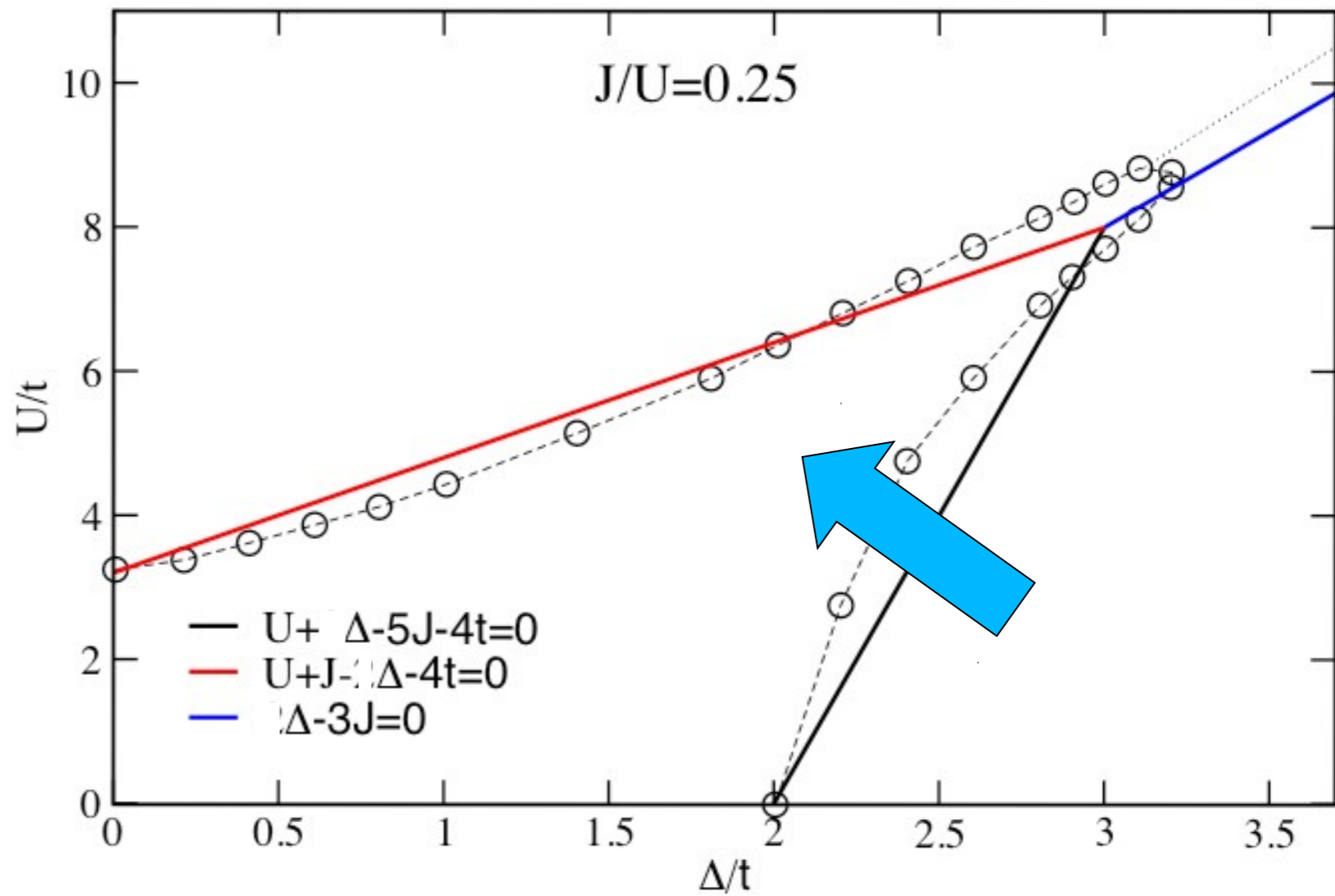
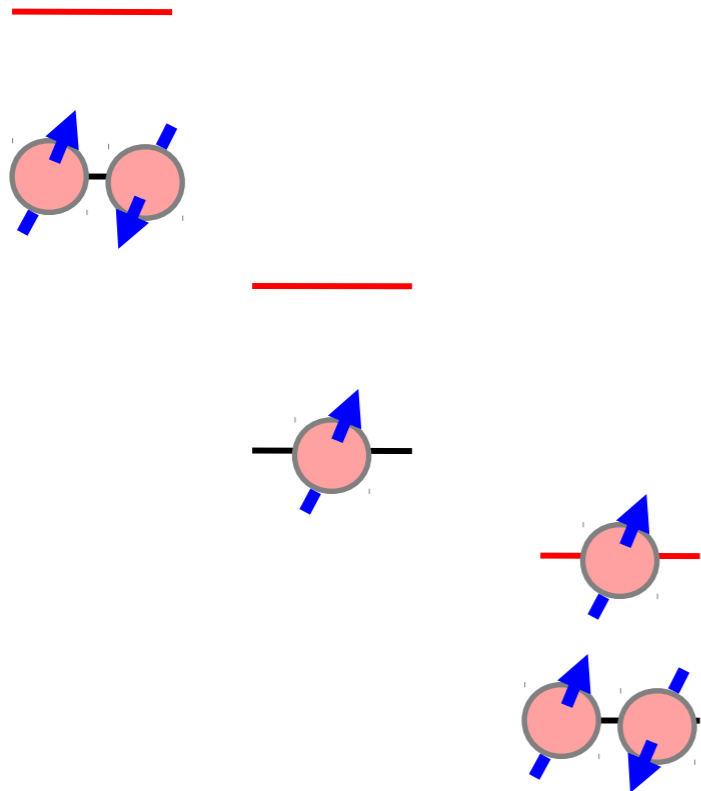
$$E_g = 2E(N) - E(N-1) - E(N+1)$$



Band gap

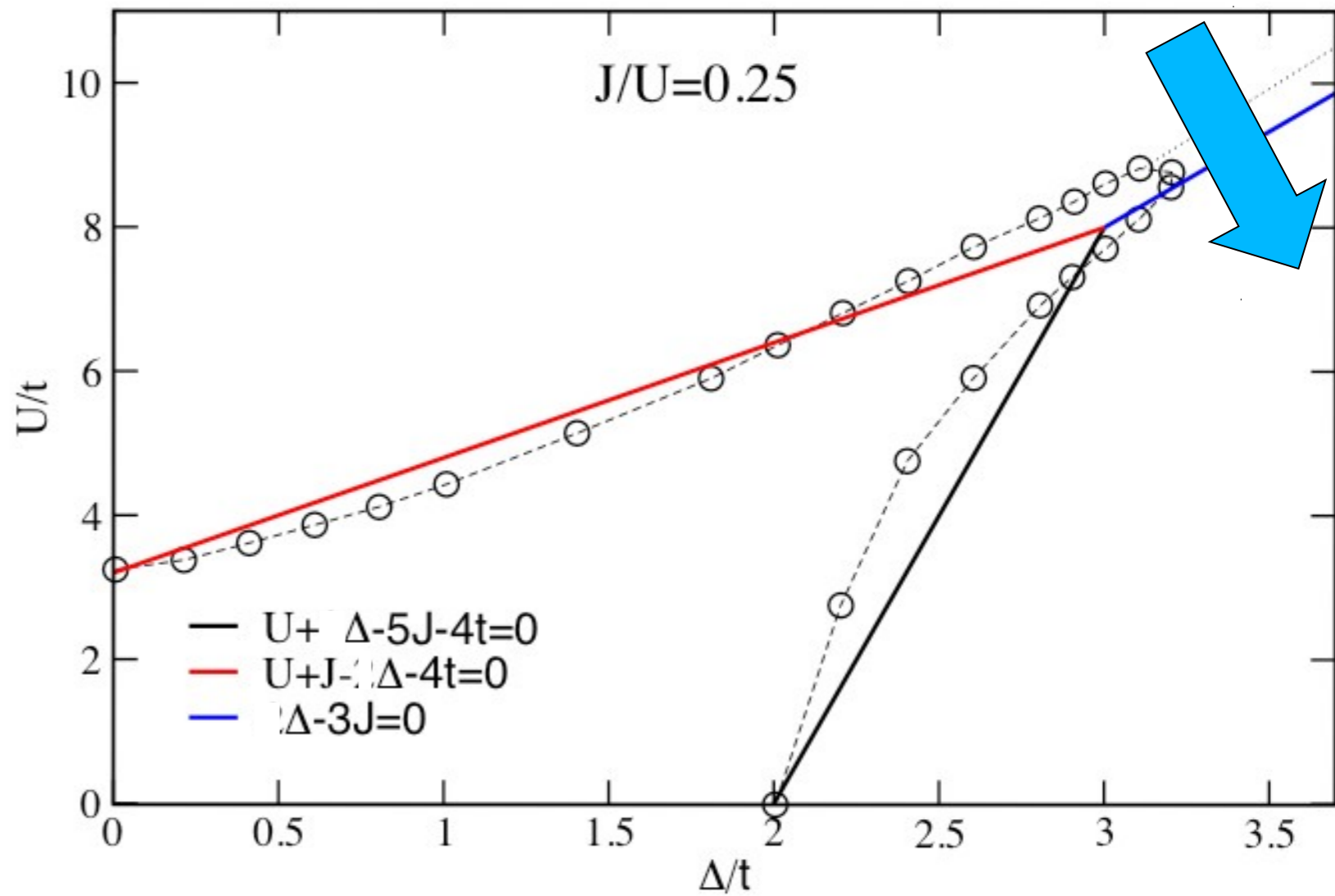
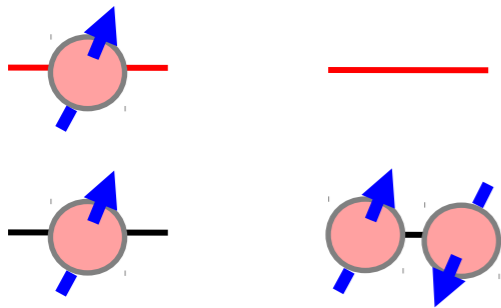
'Band gap = 0'

$$E_g = 2E(N) - E(N-1) - E(N+1)$$

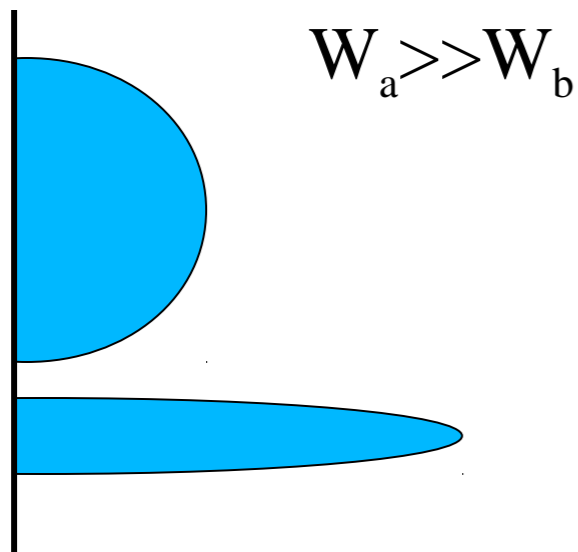


Local state transition

' $E(\text{HS}) - E(\text{LS}) = 0$ '



The model - stoichiometric filling=2e



Two sublattice order allowed

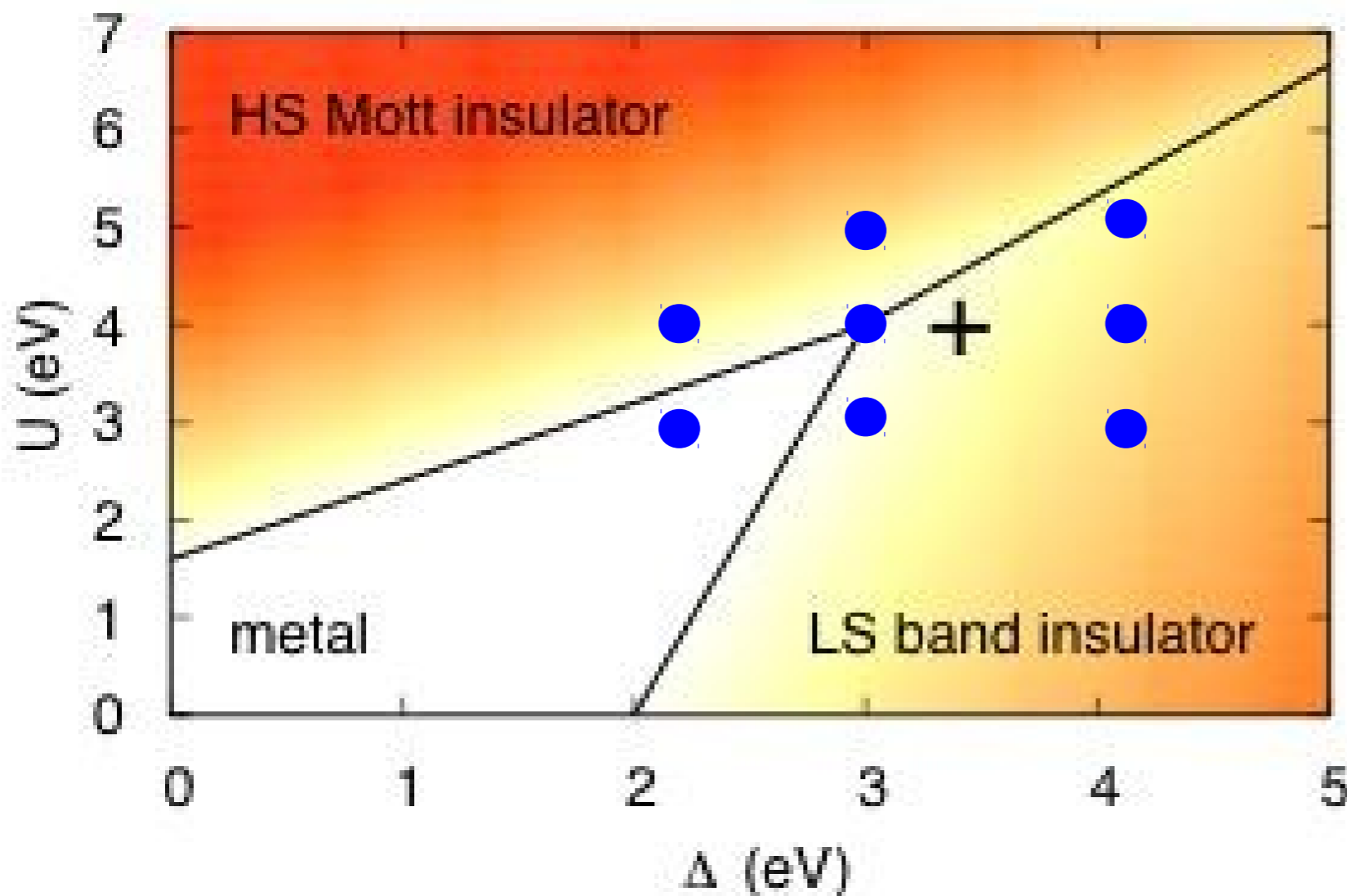
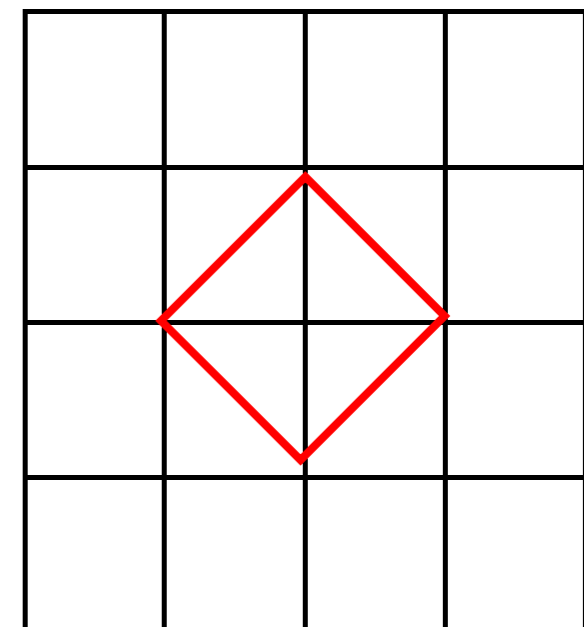
Computational parameters:

$$W_a = 3.6$$

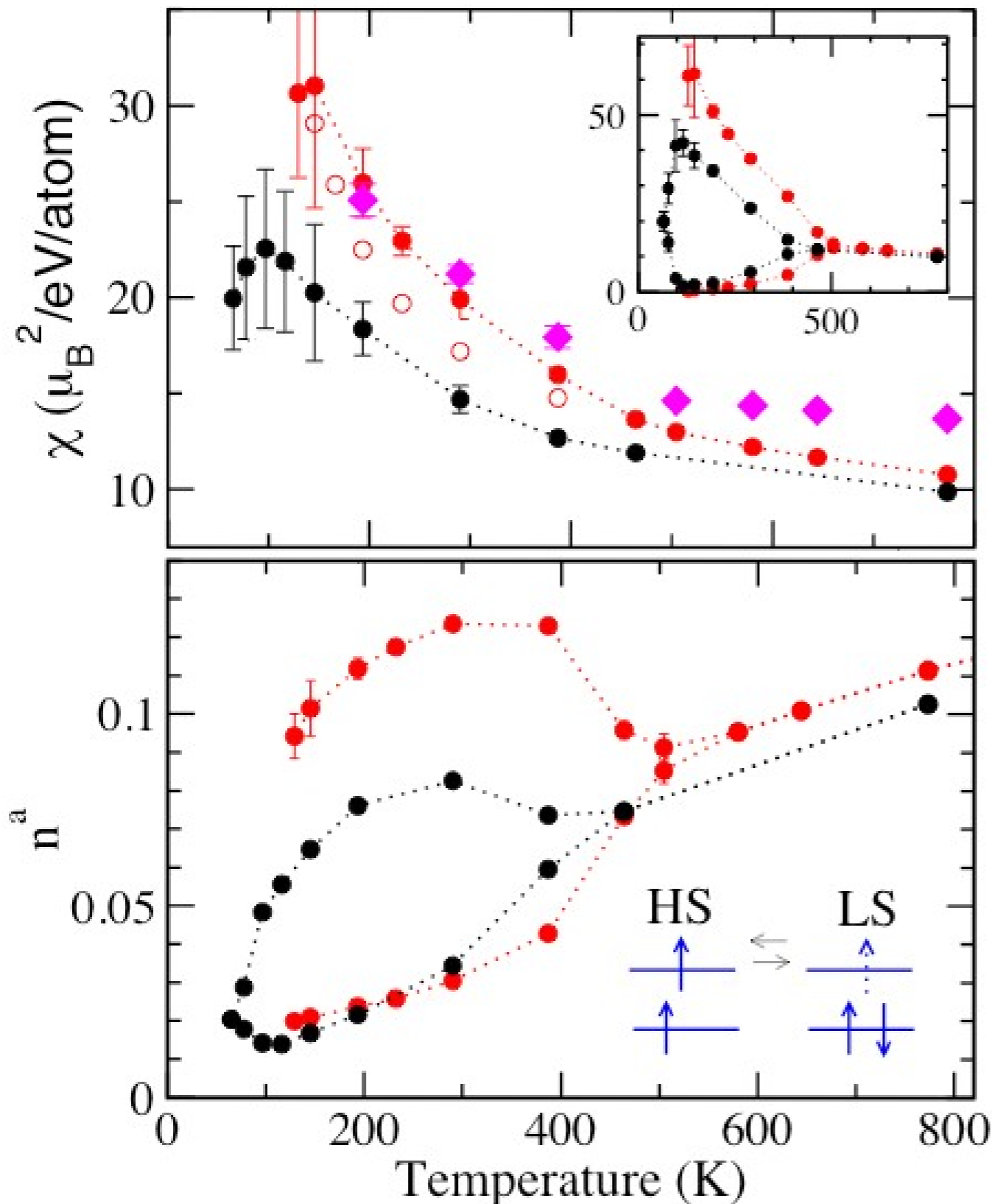
$$W_b = 0.4$$

$$U = 4, J = 1$$

Unit cell:



Spin susceptibility and disproportionation



$\Delta-3J=0.42$

local susceptibility 


$\Delta-3J=0.40$

local susceptibility 

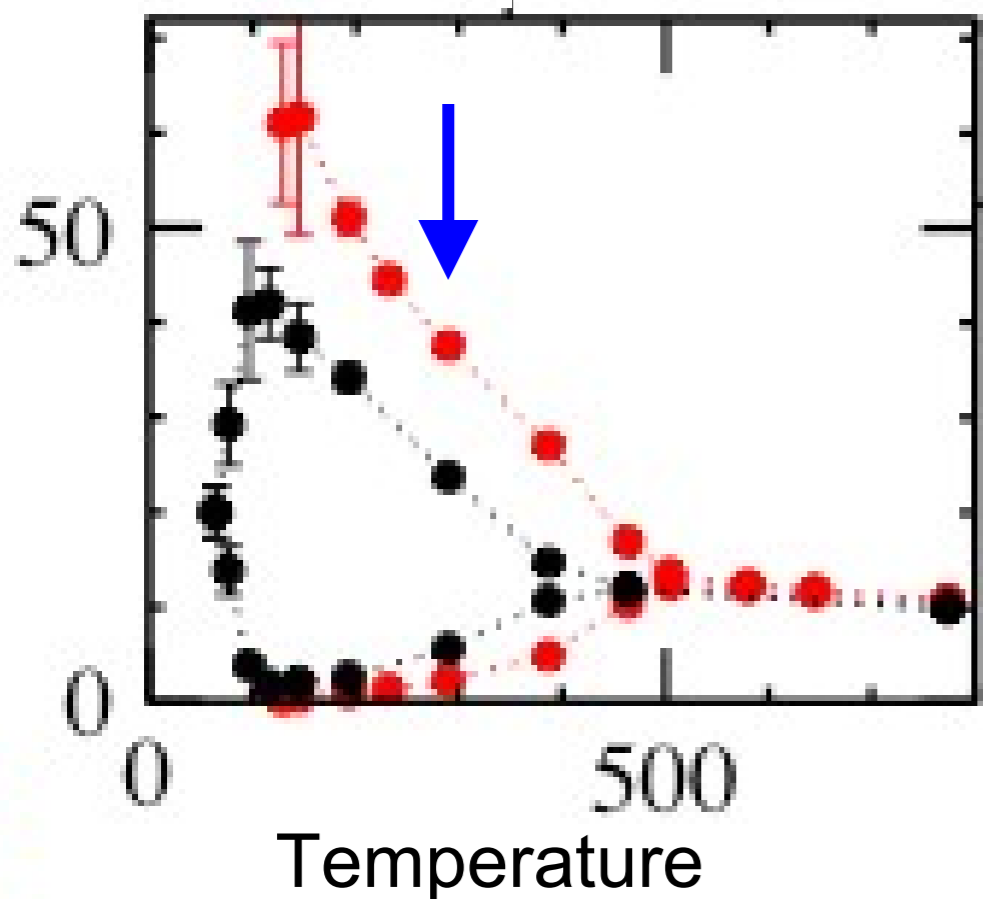
local susceptibility (homog. ph.) 

uniform susceptibility 

Site occupancy n^a (upper band)

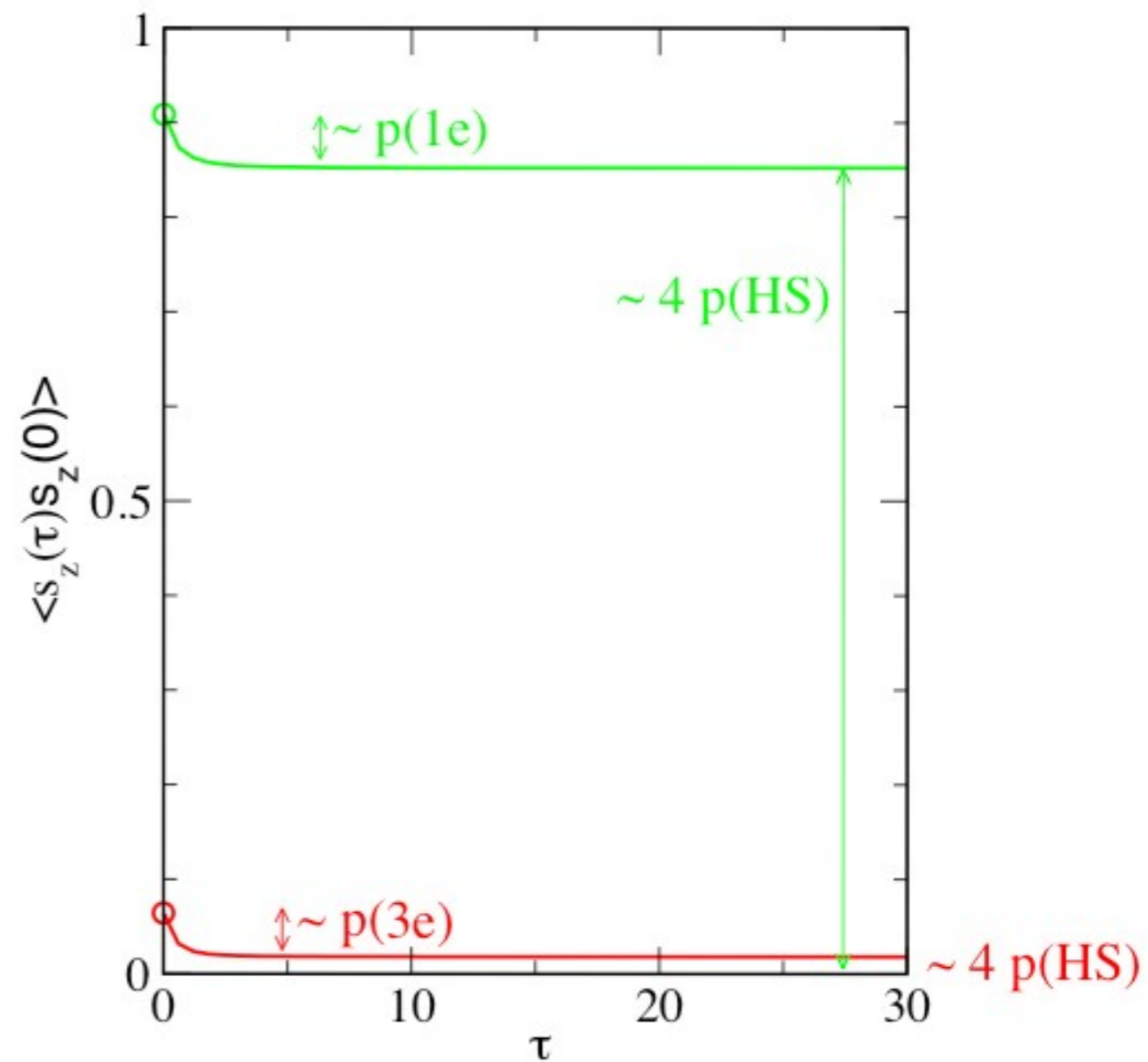
$\Delta-3J=0.42$ 

$\Delta-3J=0.40$ 

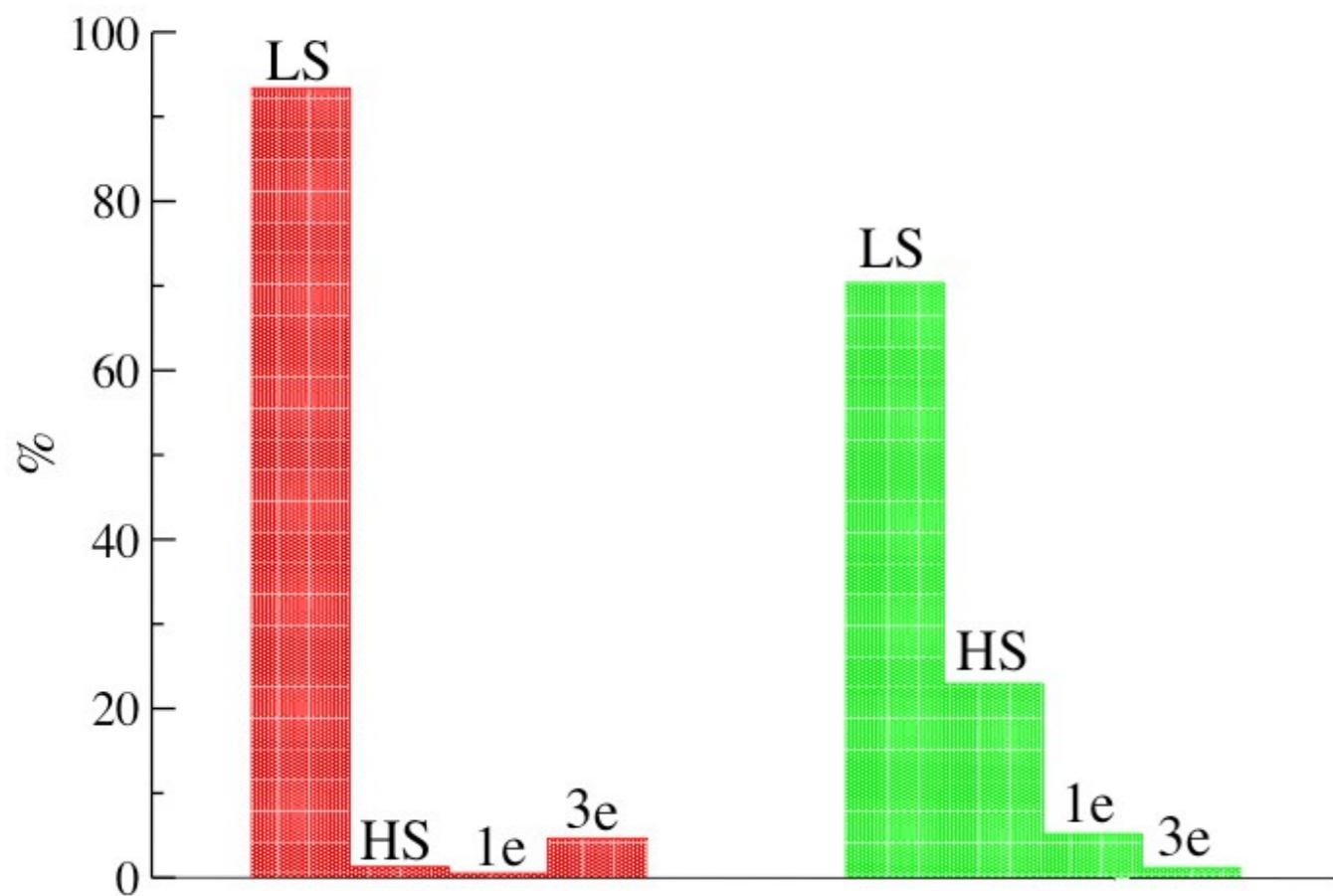


short excursions
VS
statistical mixture

Spin-spin correlations

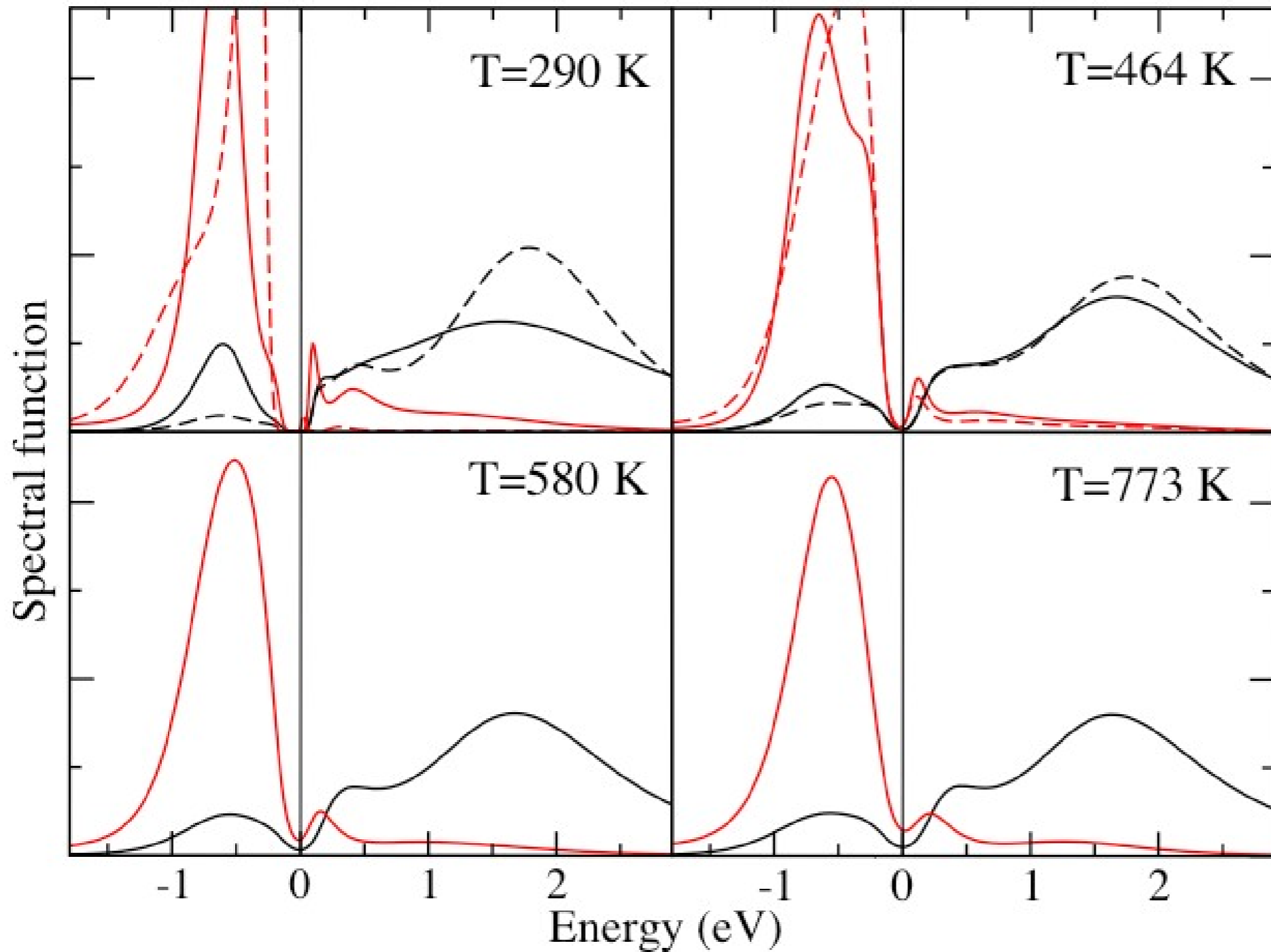


Local state statistics



One-particle spectra

$A_{aa}(\omega)$ ———
 $A_{bb}(\omega)$ ———



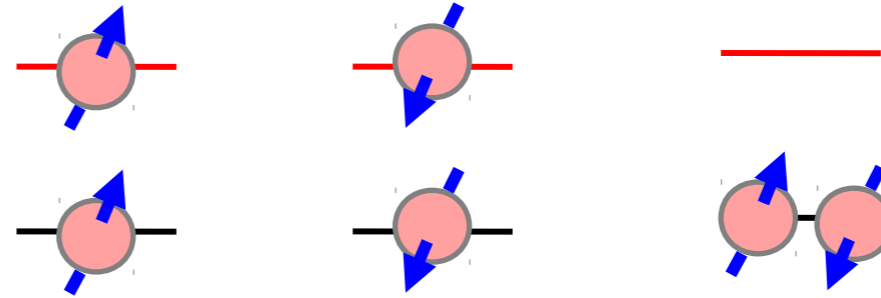
disproportionated

homogeneous

Low-energy model

Integrate out the charge fluctuations:

- keep 3 local states



- treat hopping as perturbation

Hamiltonian

$$\tilde{H} = \xi_0 \sum_{i,\sigma} n_{i,\sigma}^{\text{HS}} + \sum_{\langle ij \rangle, \sigma} (\xi_1 n_i^{\text{LS}} n_{j,\sigma}^{\text{HS}} + \xi_2 n_{i,\sigma}^{\text{HS}} n_{j,-\sigma}^{\text{HS}})$$

$$\xi_0 = \Delta - 3J, \quad \xi_1 = -\frac{t_{aa}^2}{U-2J}, \quad \xi_2 = -\frac{2t_{aa}^2}{U+J}$$

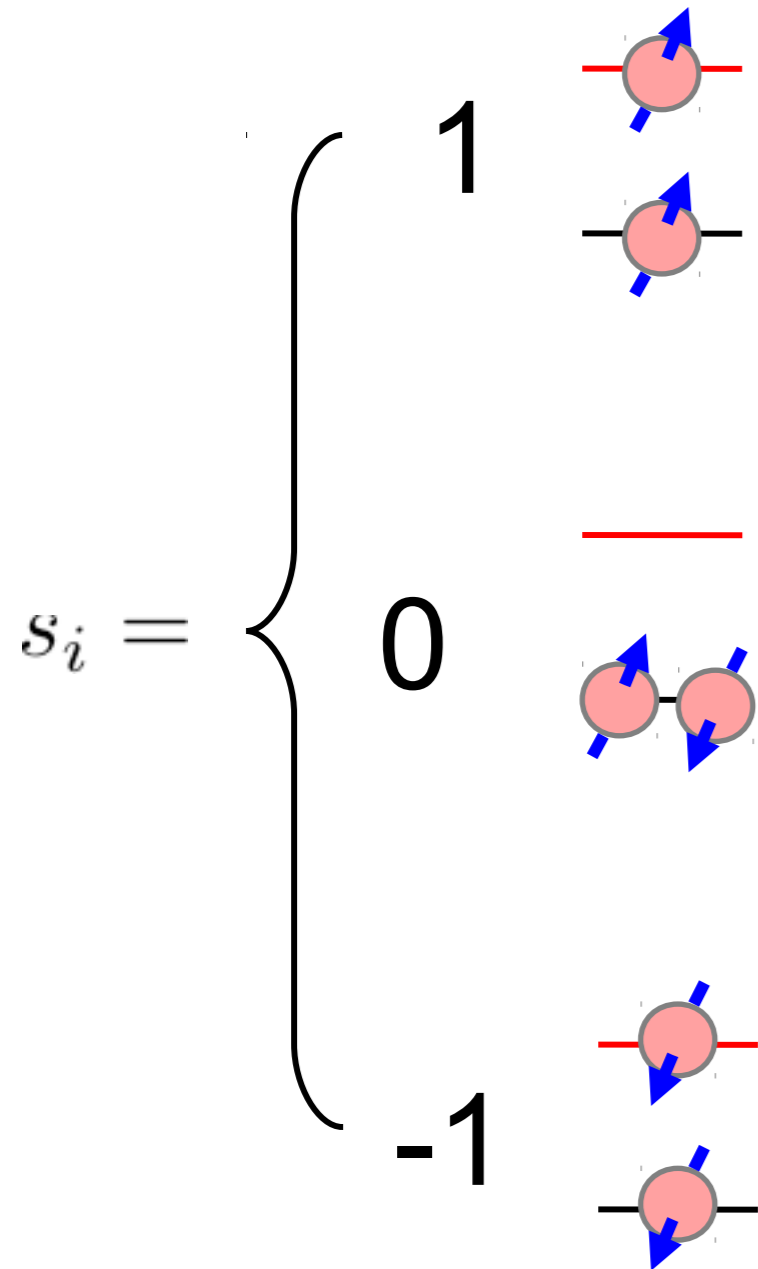
Mean-field free energy

$$\begin{aligned} F(T) = & \frac{\xi_0}{2} (x_A + x_B) + 2\xi_1 (x_A + x_B - 2x_A x_B) - \xi_2 x_A x_B \\ & + \frac{T}{2} (1 - x_A) \ln(1 - x_A) + \frac{T}{2} (1 - x_B) \ln(1 - x_B) \\ & + \frac{T}{2} x_A \ln\left(\frac{x_A}{2}\right) + \frac{T}{2} x_B \ln\left(\frac{x_B}{2}\right), \end{aligned}$$

Blume-Emery-Griffiths model

$$\tilde{H} = D \sum_i s_i^2 + K \sum_{\langle ij \rangle} s_i^2 s_j^2 + I \sum_{\langle ij \rangle} s_i s_j$$

Blume et al., Phys. Rev. A 4, 1071 (1971)

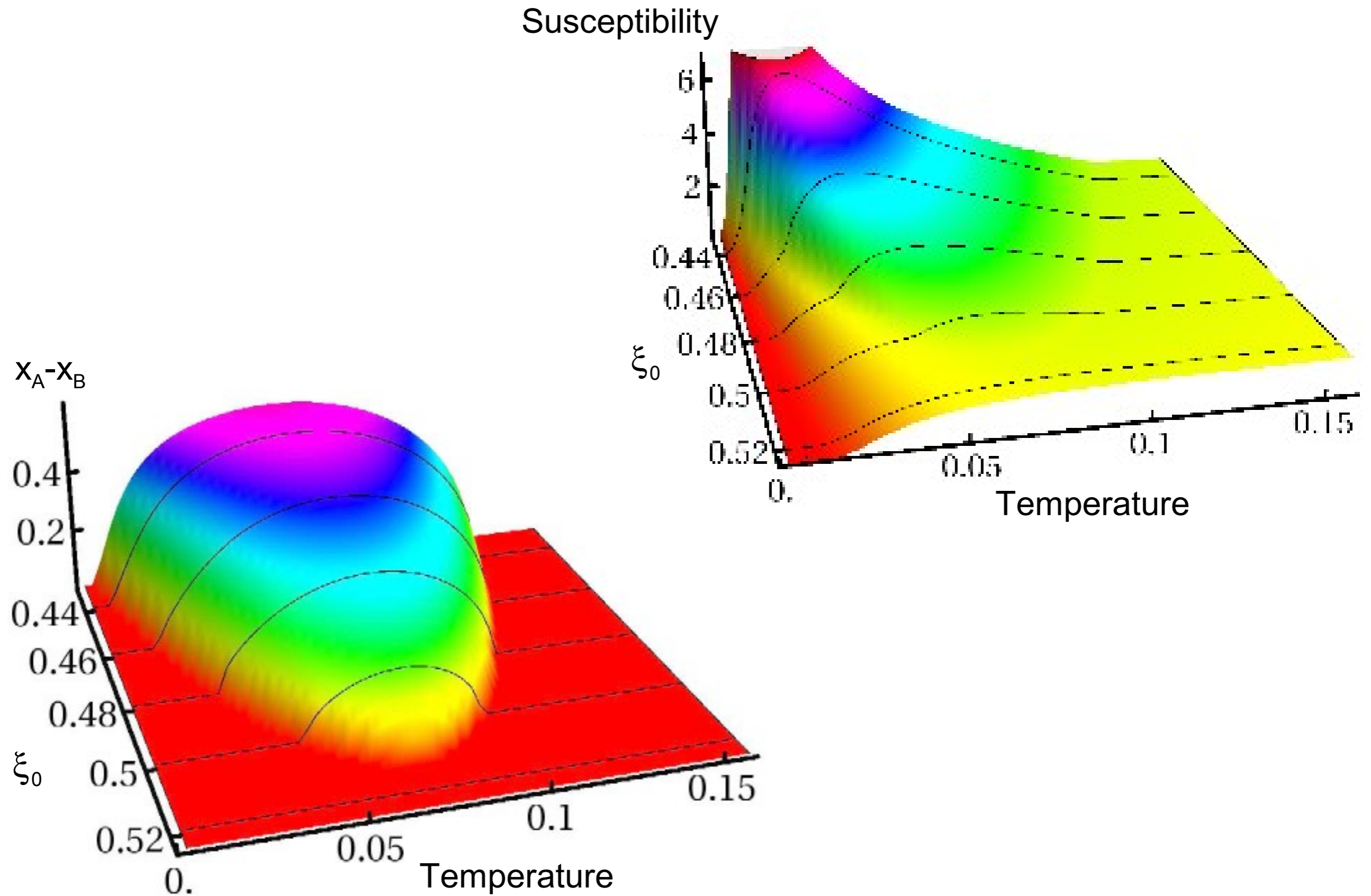


$$D = \Delta - 3J - \frac{Zt^2}{U - 2J}$$

$$K = t^2 \left(\frac{1}{U - 2J} - \frac{1}{U + J} \right)$$

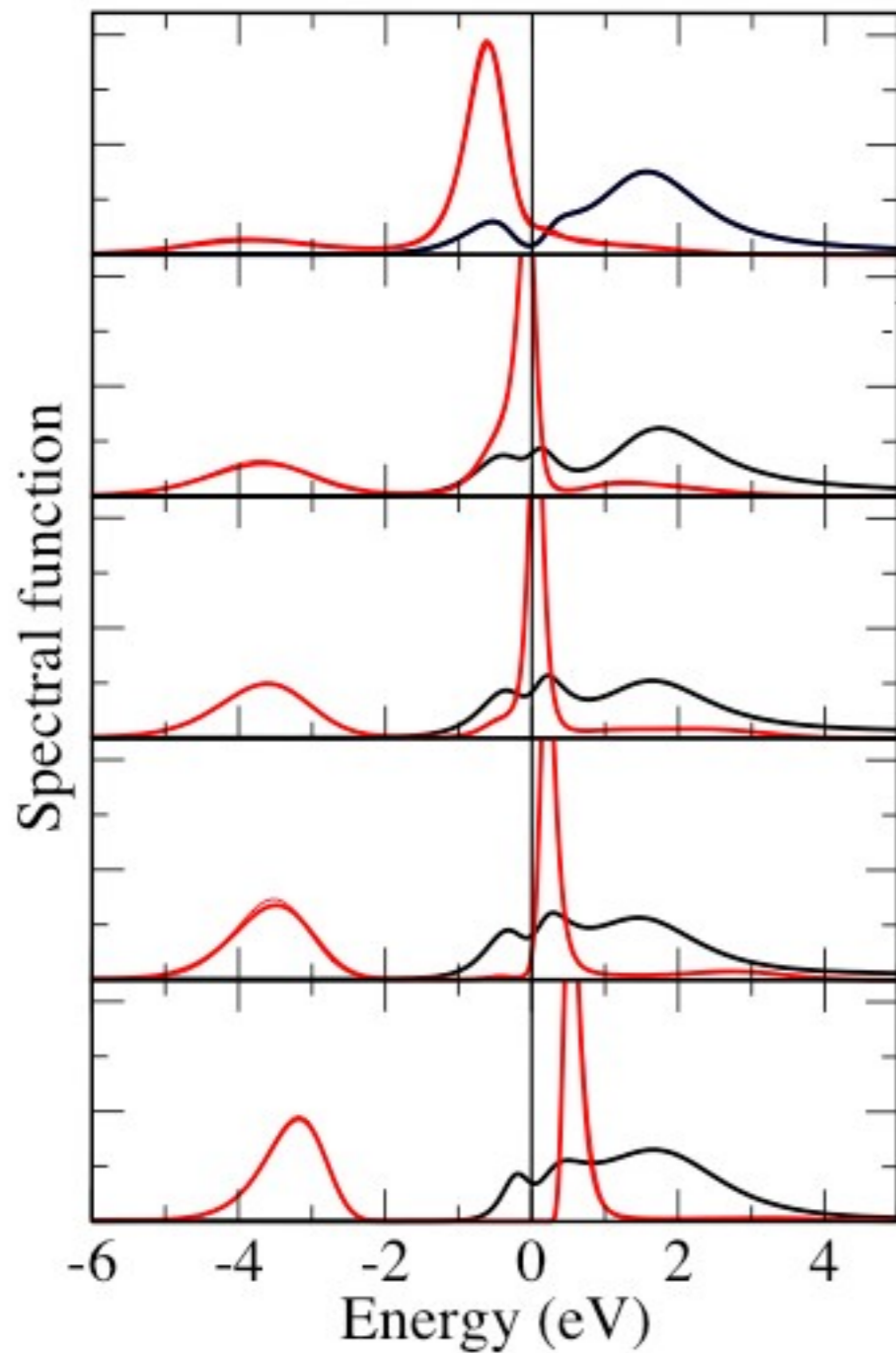
$$I = \frac{t^2}{U + J}$$

Low-energy model



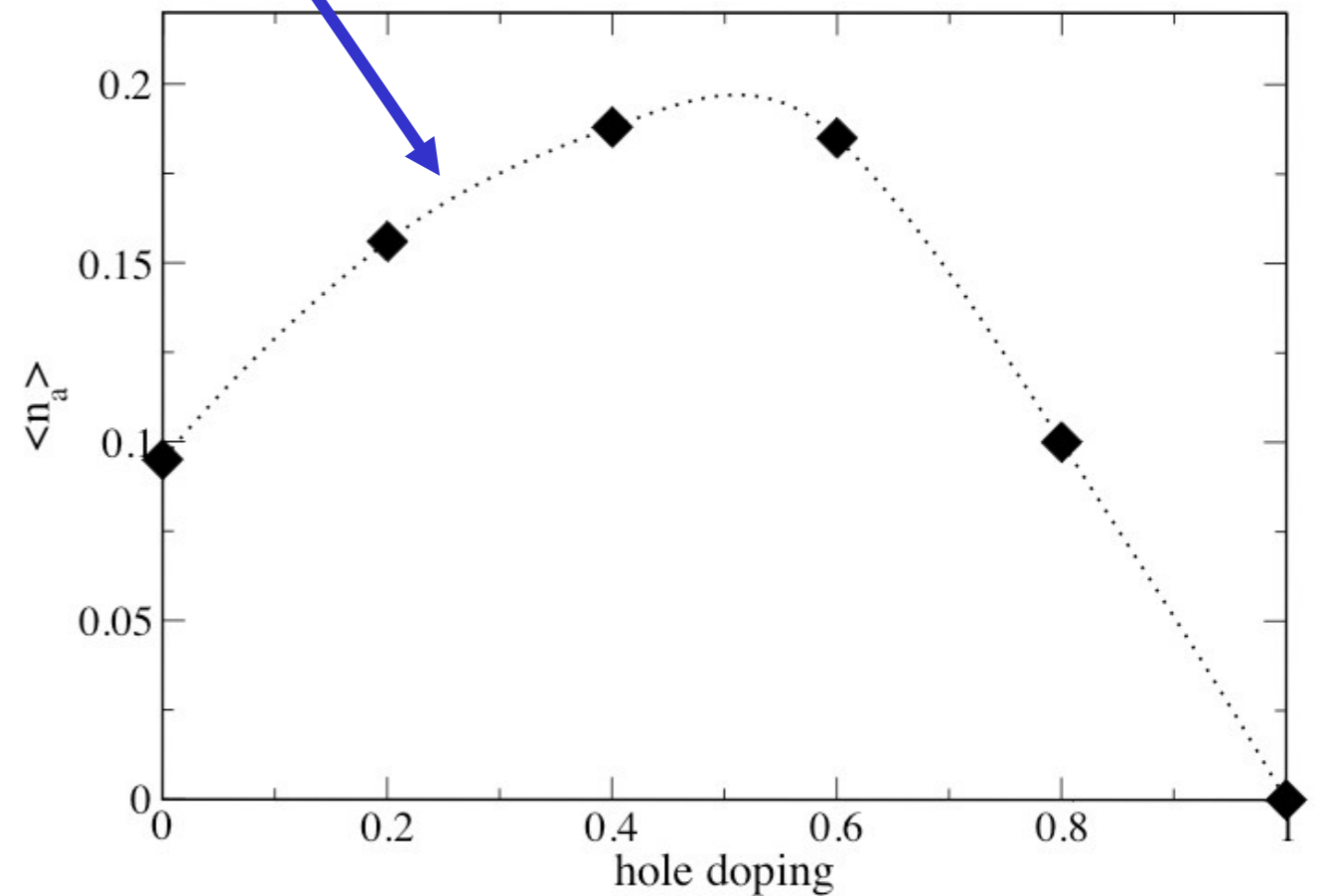
Hole doping

How do we go from localized moments to double exchange picture?

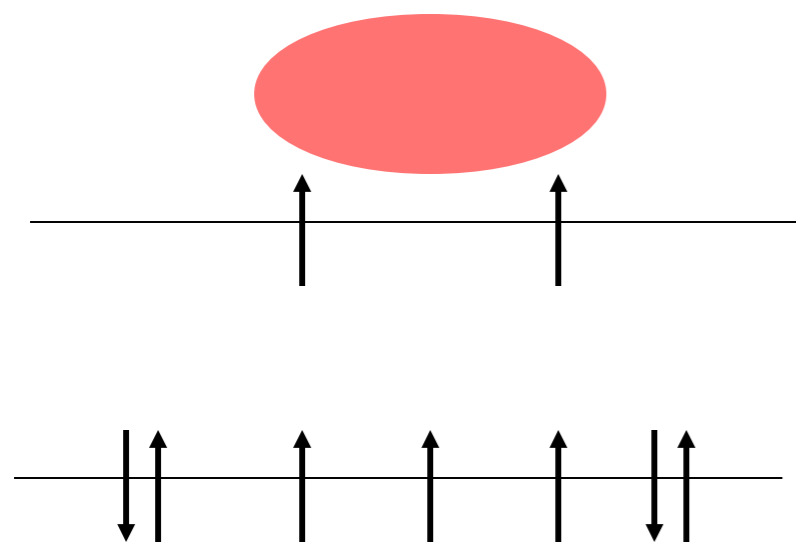
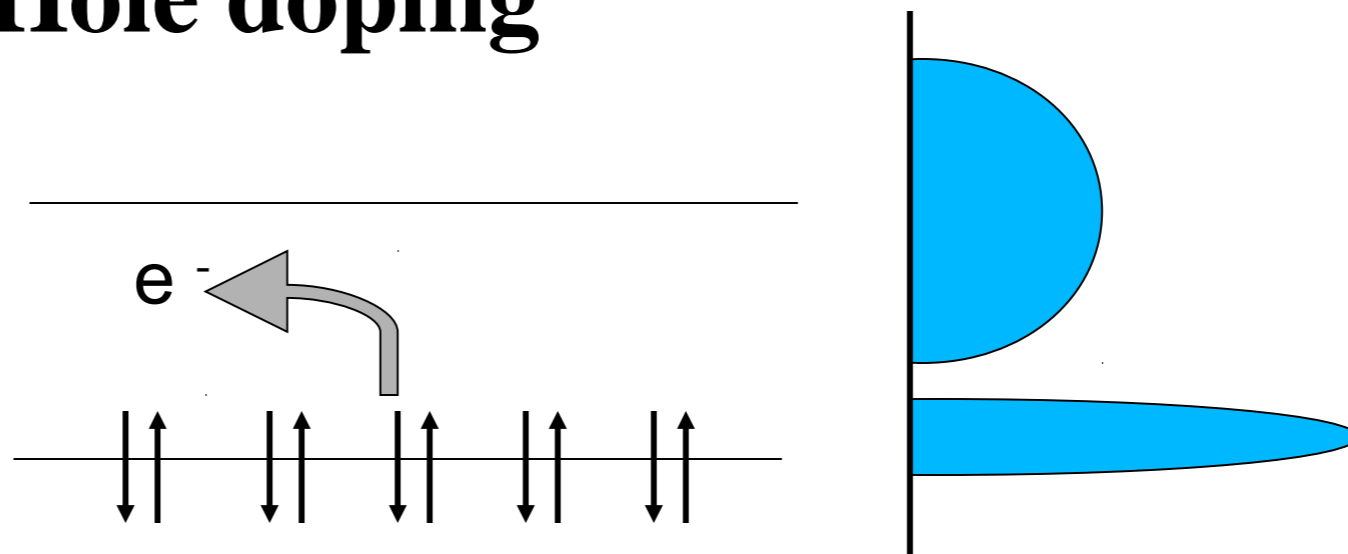


hole doping

Upper band occupancy increases !



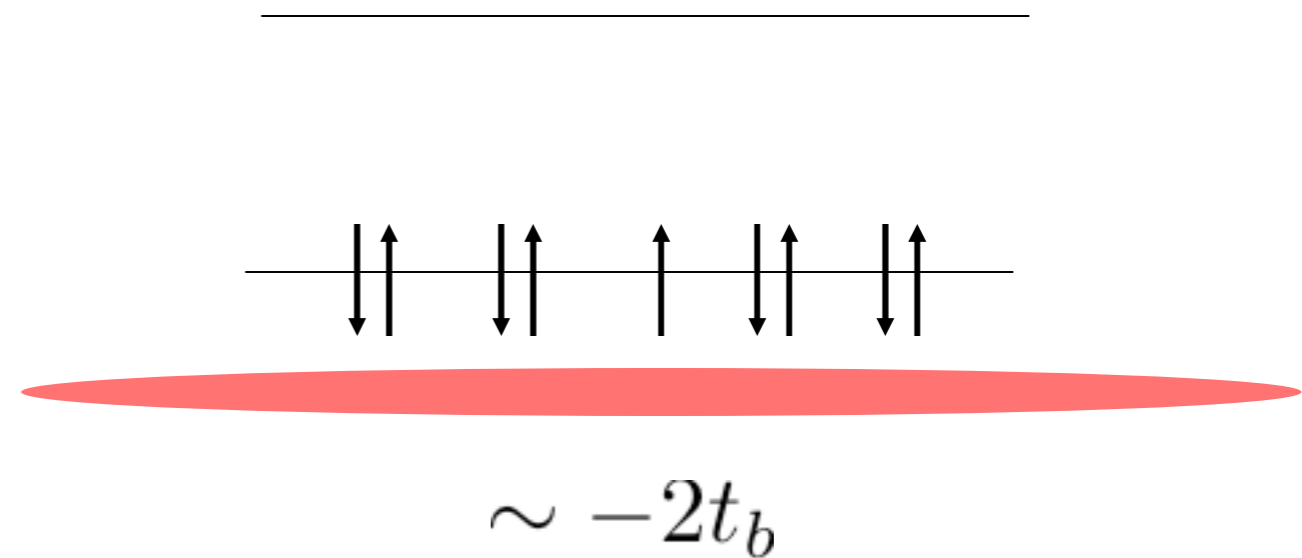
Hole doping



$$\sim -\sqrt{2}t_a + 2\xi_0$$

localized magnetic polaron

OR



$$\sim -2t_b$$

itinerant hole in lower band

Conclusions

- (Quasi)degeneracy of ionic multiplets leads to rich phase diagrams in strongly correlated systems.
- Effective HS-LS attraction at the HS/LS transitions leads to a ordered state with reduced translational symmetry.
- 2-band Hubbard model with crystal field provides fermionic realization of BEG model and introduces new parameter - doping
- Under certain circumstances ($W_a \gg W_b$) doping leads to formation of inhomogeneities - magnetic polarons